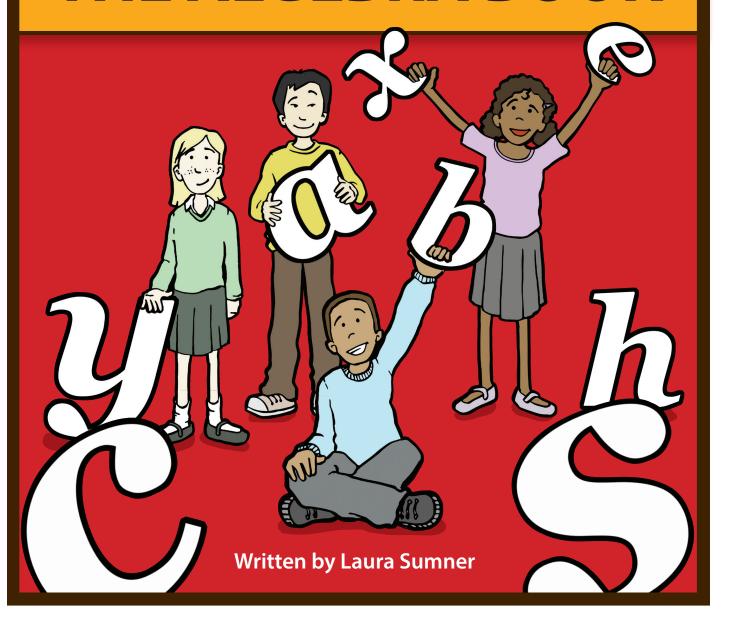
# Head Start primary

# THE ALGEBRA BOOK







# THE ALGEBRA BOOK

Written by Laura Sumner



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# HeadStart Primary: THE ALGEBRA BOOK Introduction

#### Rationale and book organisation

These questions have been written in line with the objectives from the Mathematics Curriculum.

Algebra is not included as a separate content domain until the Year 6 Programme of Study, when children are expected to use letters to represent unknown numbers. However, the concepts which children need to grasp in order to gain a full understanding of algebraic principles are developed within the mathematics curriculum from Year 1.

**Part 1** (page 1 - 36) of this book is based on pre-Year 6 expectations and provides teachers with the opportunity to revise those concepts at an appropriate level for Year 6 pupils. Therefore, it is expected that teachers will use the first part of the book, as necessary, for the whole class or groups of children. It may be that teachers decide to give the earlier pages as homework, prior to beginning the Algebra topic. Alternatively, Part 1 can be used in earlier year groups in preparation for Year 6, as appropriate.

**Part 2** is based on the Year 6 expectations and includes questions to reflect all the Year 6 objectives from the Mathematics Curriculum Algebra content domain. In addition, 'using the correct order of operations' (taken from the Year 6 Number – addition, subtraction, multiplication and division domain) and 'solving equations with an unknown number on both sides' (challenge beyond that expected within the Year 6 curriculum) is applied to algebra.

#### Approaches to teaching algebra

In order to support the teaching of algebraic concepts, reminders of appropriate strategies, which model important principles in algebra, are identified on some pages. It is understood that schools may vary their teaching approach from the model shown. In such cases, teachers should substitute the appropriate school model.

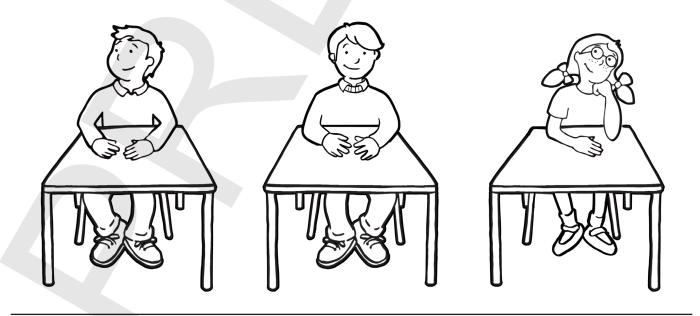
When multiplying in algebra, common practice is to omit the multiplication symbol. However, so that children can focus on the concept of letters representing missing numbers, the early pages within the Year 6 Expectations do include the symbol. Later pages introduce the practice of omitting the multiplication symbol.

#### Differentiation

In general, the questions are arranged so that they become progressively more difficult on each page. Additionally, for each objective, there is a page or pages which give the opportunity to practise the objective at a standard level (relatively simple calculations e.g. smaller numbers, limited crossing of the tens boundary etc.), as well as a parallel page or pages at a more challenging level (more complex calculations, larger numbers etc.). This is indicated by (th) at the bottom right hand corner of the page. Consequently, to aid differentiation, those children who need to focus purely on the algebraic concepts are able to work on relatively simple calculation aspects, whilst those children who are capable of understanding algebra with more challenging calculations are also provided for. It may be appropriate for some children to attempt the simpler pages before moving on to the challenging pages. The last objective 'Solve equations with an unknown number on both sides', only contains challenging pages as the concept covers challenge beyond that expected within the Year 6 curriculum.

### Using the worksheets

The book is designed so that children are able to write answers on the photocopied sheets, which may be particularly useful if given as homework. However, should it be more appropriate, pupils can easily transcribe the work into exercise books. Where substantial 'working out' needs to be completed, this may have to be carried out in exercise books or on separate paper.



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# **Year 6 Expectations**

#### Part 2: Year 6 (and beyond) Expectations (continued)

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# Part 1 **Pre-Year 6 Expectations** This section will help you prepare to study algebra!



# Use the relationship between addition and subtraction to solve missing number problems.

1 Complete the following.

+ 4 = 9

+ 33 = 76

**b** 6 + = 13

e 146 + = 259

**C** 26 + = 87

+ 222 = 334

2 Now try these.

a 15 - = 11

-42 = 57

**b** - 3 = 16

e 174 – = 62

**C** 32 - = 24

-85 = 110

3 Have a go at these.

a 14 + = 76

-121 = 57

-37 = 51

e 232 + = 496

**C** 23 + = 84

**f** - 236 = 151

Name.....

Class.....

Date.....

Use the relationship between addition and subtraction to solve missing number problems.

1 Complete the following.

$$+ 752 = 934$$

2 Now try these.

$$-53 = 26$$

$$-89 = 47$$

$$-2085 = 289$$

**3** Have a go at these.

$$-246 = 178$$

$$-1187 = 3539$$

Class..... Date....

## Use the relationship between addition and subtraction to solve missing number problems.

Complete the following by filling in all the boxes with the numbers from the first equation. An example is shown.

a 13 54 67 + SO 54 13 67 +67 13 and 54

> and 67 13 54

b 52 85 33 = SO 85 and 85 +=

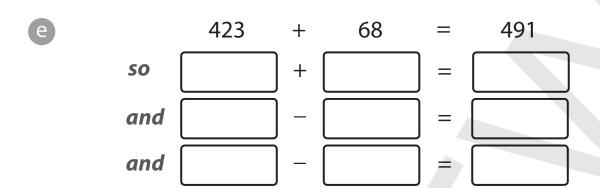
> and +

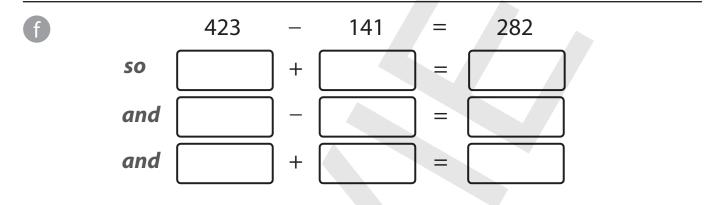
168 C 144 24 SO 168 = and + =

and =

d 127 83 44 =50 127 +and += and =

Name...... Date...... Date......





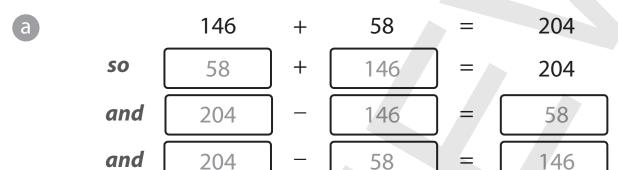
$$306 + 124 = 430$$
 $50 - =$ 
 $and - =$ 
 $and + =$ 

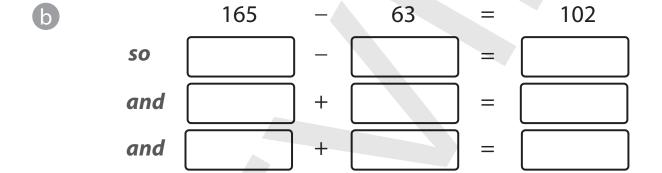
You're doing really well!

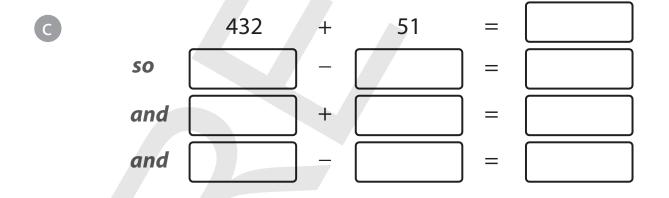
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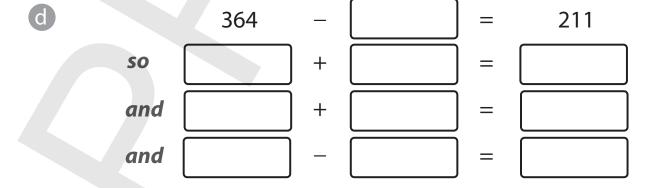
# Use the relationship between addition and subtraction to solve missing number problems.

1 Complete the following by filling in all the boxes with the numbers from the first equation. An example is shown.

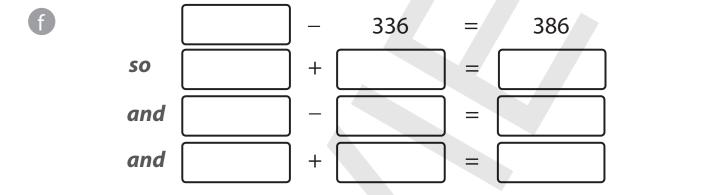








е		356	+	=	862
	50		+	=	
	and [		_		
	and		_	=	







Use the relationship between addition and subtraction to solve missing number word problems.

- 1 Read each problem below. **Put a circle** around the equation you would use to solve the problem.
- There are 56 blue and red cars in the garage. 23 are blue. How many red cars are there?

Mrs Shah baked 86 cakes for her daughter's birthday party. After the party, 25 were left. How many cakes were eaten at the party?



From Monday to Thursday, Esme collected 43 house points. On Friday she gained another 14. How many house points did Esme collect altogether?

- 2 Now try this
- a Before lunch, Ruthie drove 56 miles. After lunch she drove 27 miles. How many miles had she driven altogether?



b Use the equation you have chosen to find the answer to the problem.

- **3** Have a go at this one.
- Tom got his spending money on Saturday. He spent £3.50 at the shop and had £5.00 left. How much spending money had Tom received?

$$£3.50 + £5.00 = ?$$

$$£5.00 + ? = £3.50$$

$$£3.50 - £5.00 =$$
?

$$£5.00 - £3.50 =$$
?

b Use the equation you have chosen to find the answer to the problem.

£

Na	me	Class	Date
4	For these problems, write down and the state of the state		o solve the problem.
a	65 people were on the bus. Some moff. Then there were 82 people on the		
	You can use this space for your work	king.	
b	A shop had 79 iPads. On Monday it have left?	sold 23 iPads. How man	y iPads did the shop
	You can use this space for your work	king.	
C	The classroom library had 126 book on the library book shelves?	ss. 42 were out on loan. I	How many books were
	You can use this space for your wor	king.	

### Use the relationship between addition or subtraction to solve missing number word problems.

- 1 Read each problem below. **Put a circle around** the equation you would use to solve the problem.
- a Afzal had 182 football cards altogether. 73 had a picture of a premiership player. How many cards did not have a picture of a permiership player?



Mr Bread, the baker, sold 473 loaves, on Monday. On Tuesday he sold 189 loaves. How many loaves did Mr Bread sell altogether?

Jan's netball team scored 256 goals during the season. They had 79 goals scored against them. What was the difference between the goals for and against?

**ALGEBRA** 

- 2 Now try this
- Janey's family had to drive 1652 kilometres to their holiday destination. On the first day, they drove 967 kilometres. How much further did they have to drive?

b Use the equation you have chosen to find the answer to the problem.



- **3** Have a go at this one.
- a 1908 pupils attend Sunnyside High School. 1184 are boys. How many are girls?



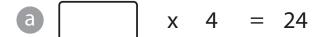
b Use the equation you have chosen to find the answer to the problem.



Na	me Date Date
4	For these problems, write down an equation you could use to solve the problem. Then use your equation to find the answer.
а	Anya was saving up for a laptop. She saved £375.50 from her earnings and £50.78 from her birthday money. How much did Anya save altogether?
	£
	You can use this space for your working.
b	The perimeter of a garden measured 156.35m. There was a fence aound 78.5 metres of the perimeter. How much of the garden's perimeter did not have a fence?
	You can use this space for your working.
C	To arrive at their holiday destination, Julian's family drove 87km before lunch and 87km after lunch. How far did they drive altogether?
<u></u>	You can use this space for your working.

# Use the relationship between multiplication and division to solve missing number problems.

1 Complete the following.



x 7 = 42

**b** 6 x 
$$= 30$$

f 8 x = 96

2 Now try these.

e 84 ÷ = 7

3 Have a go at these.

a 
$$x = 5 = 40$$

e 9 x = 108

# Use the relationship between multiplication and division to solve missing number problems.

1 Complete the following.

$$x 12 = 84$$

$$x 14 = 728$$

$$x 15 = 180$$

2 Now try these.

$$\div$$
 12 = 8

$$\div 30 = 76$$

$$\div 53 = 91$$

**3** Have a go at these.

$$x 30 = 930$$

$$\div 42 = 23$$

Class..... Date...

## Use the relationship between multiplication and division to solve missing number problems.

1 Complete the following by filling in all the boxes with the numbers from the first equation. An example is shown.

a		8	X	7	=	56
	so	7	] x [	8	=	56
	and	56	÷	7	=	8

56

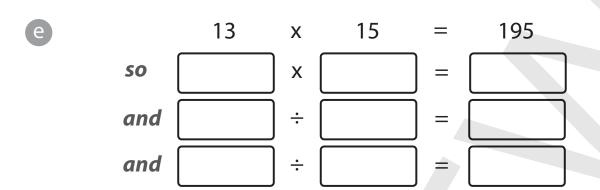
b		54	÷	9	=	6
	so	54	÷		=	9
	and		X		=	54
	and		X		=	

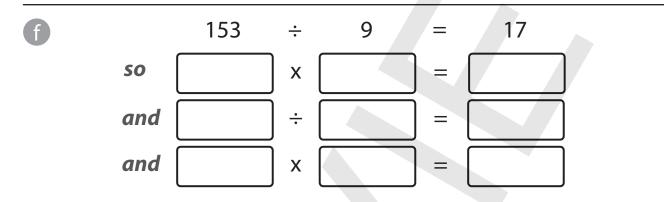
C		12	X	8	=	96
	so	96	÷		=	
	and		X		=	
	and		÷		=	

d		78	·	6	=	13
	50		x		=	78
	and		X		=	78
	and		÷			

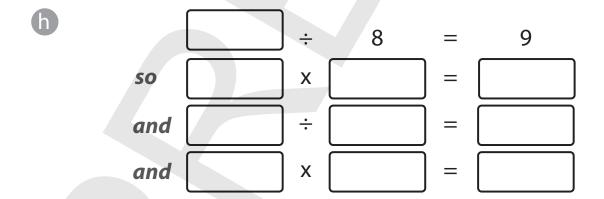
and

Name...... Date...... Date......





g		23	X	12	=	276
	so		$\Big]  \div  \Big[$		=	
	and		) ÷ [		=	
	and		) x [		=	



You're doing a great job!

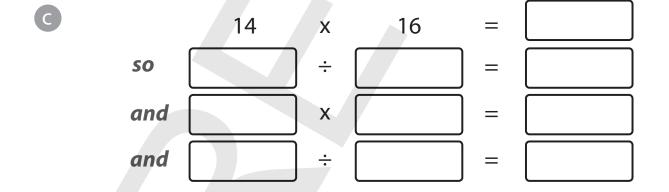
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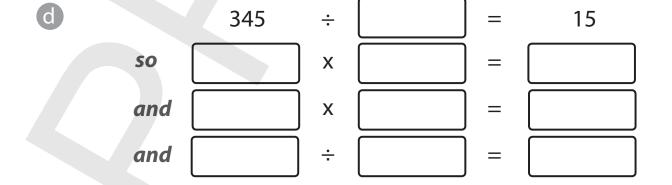
# Use the relationship between multiplication and division to solve missing number problems.

1 Complete the following by filling in all the boxes with the numbers from the first equation. An example is shown.

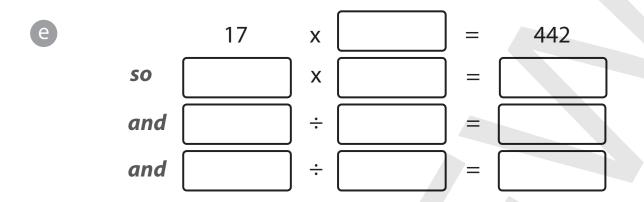
a		13	X	21	=	273
	so	21	X	13	= _	273
	and	273	÷	13	=	21
	and	273	<u>÷</u>	21	=	13

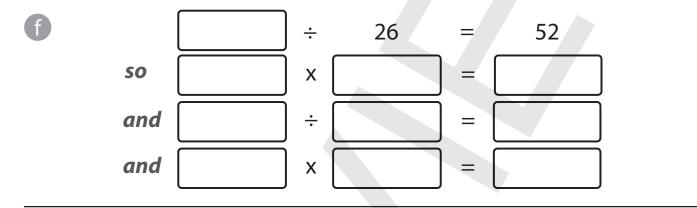
b		322	÷	14	=	23
	so		$]$ $\div$		=	
	and		X			
	and		x		=	

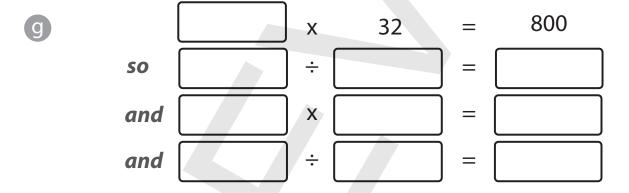


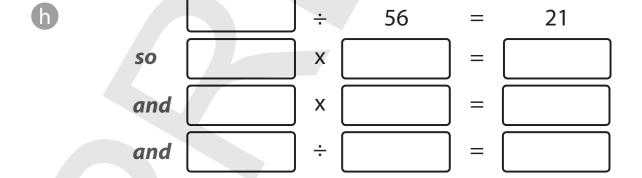


Name...... Date...... Date.....









Keep up the good work!

## Use multiplication or division to solve missing number word problems.

- 1 Read each problem below. Put a circle around the equation you would use to solve the problem.
- a Baz, Gracie and Shazia share £27 evenly between themselves. How much does Gracie get?

$$3 \times £27 = ?$$

£27 
$$\div$$
 3 =  $?$ 

$$3 \div £27 = ?$$

b In the reception class, there are ten books in each reading box. There are eight reading boxes. How many books are there altogether?



$$10 \times 8 = ?$$

Six friends had £2.50 each to go to the fair. How much had they altogether?

$$6 x ? = £2.50$$

£2.50 
$$\div$$
 6 =  $?$ 

£2.50 
$$\times$$
 6 = ?

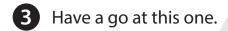
$$6 \div £2.50 = ?$$

- 2 Now try this
- a Katya thought of a number and divided it by 9. Her answer was 12. What was Katya's number?

$$9 x ? = 12$$



b Use the equation you have chosen to find the answer to the problem.



Amir had the same number of marbles in each of 8 tubs. He had 56 marbles altogether. How many marbles were in one tub?



b Use the equation you have chosen to find the answer to the problem.

Na	ame	Class	Date					
4	For these problems, write down an ed Then use your equation to find the ar		o solve the problem.					
a	Six friends each gave the same amount to the school charity fund. They gas altogether. How much did they each give?							
	You can use this space for your worki	ng.						
	4							
b	Laura, Riz and Chloe each swam 23 ler swim altogether?	ngths of the pool. How r	nany lengths did they					
	You can use this space for your worki	ng.						
		a line						
C	Brenda's Bakery sold 27 loaves of brea they sell altogether?	d every day for 6 days. H	low many loaves did					
	You can use this space for your worki	ng.						

## Use multiplication or division to solve missing number word problems.

- 1 Read each problem below. Put a circle around the equation you would use to solve the problem.
- Seven people bought a ticket for a fairground ride. They paid £21.70 altogether. How much did each ticket cost?

£21.70 x 
$$7 = ?$$

$$7 \div £21.70 = ?$$

$$7 \times £21.70 = ?$$

Archie saves £1.50 per week for 56 weeks. How much did he save altogether?



$$?$$
 x £1.50 = 56

£1.50 
$$\div$$
 56 =  $?$ 

£1.50 
$$\times$$
 56 =  $?$ 

A shop sells 592 bars of chocolate over 16 days. What is the average number of bars sold per day?

- 2 Now try this
- Asmat thought of a number and divided it by 18. His answer was 21. What was Asmat's number?



b Use the equation you have chosen to find the answer to the problem.

- **3** Have a go at this one.
- The pasta factory divided pasta between 56 bags with 55 grams in each bag. How much pasta was there to start with?

$$55g x ? = 56$$

$$55g \div 56 =$$
?

$$56 x 55g =$$
 ?

b Use the equation you have chosen to find the answer to the problem.

g

Name	Class	Date					
For these problems, write down an Then use your equation to find the		o solve the problem.					
a A box can hold 12 biscuits. How ma	ny boxes are needed to h	old 768 biscuits?					
You can use this space for your wor	king.						
b Mo's teacher asked, "If a number divi should Mo's answer have been?	ided by 32 is 98, what is th	e number?". What					
You can use this space for your wor	king.						
	An average of 872 people attended the local football team's matches over 22 gam during a season. How many people attended altogether?						
	=						
You can use this space for your wor	king.						

# Understand that any symbol can be used to represent numbers.

**KEY** 





$$=$$
 5

$$54$$

Use the key above to solve the following.









2 Now try these.













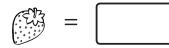
























Class..... Date .....

# Understand that any symbol can be used to represent numbers.

**KEY** 









Use the key above to solve the following.























2 Now try these.











































Understand that any symbol can be used to represent numbers. Use the relationships between operations.

KEY







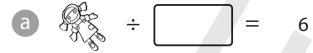
$$=$$
 5

1 Use the key above to solve the following.





2 Now try these.



$$x = 55$$

Name.....

Class.....

Date .....

Understand that any symbol can be used to represent numbers. Use the relationships between operations.

KEY







1 Use the key above to solve the following.

2 Now try these.

$$= 204$$

$$= 6945$$

$$b = 812$$

$$-$$
 = 864

$$\div \qquad = \qquad 63$$

#### Make both sides of an equation equal, where one side contains a missing number

1 Complete the following.

**b** 
$$27 - 9 = \boxed{-4}$$

$$9 81 \div \boxed{\phantom{0}} = 54 \div 6$$

h 8 x 13 = 
$$x 2$$

$$-28 = 72 - 34$$



Name...... Date..... Date.....

2 Now try these.

3 x 2 = 
$$\div$$
 5

d 
$$96 \div 8 = x \cdot 4$$

$$+ 15 = 34 - 7$$

$$9 \ 2 \ x = 72 \div 9$$



Name...... Date...... Date......

3 Have a go at these. They may be tricky - look carefully at the operations!

**b** 
$$54 \div 9 = \boxed{ -23}$$

$$d 7 + 5 = \div 2$$

$$h 96 \div 3 = 17 +$$



Name ...... Date ......

4 Now try these. Think carefully.

(a) 
$$23 + 49 = 8 \times$$
  $= 104 - 32$ 

$$\bigcirc 105 \div 3 = 7 \times 5 = 18 + \bigcirc$$

d 
$$360 - 296 =$$
  $\div 8 = 25 + 39$ 

e 
$$56 + 32 =$$
  $x 11 = 176 \div 2 =$   $-14$ 

g 6 x 23 = 150 - 
$$\left[ \right]$$
 = 276 ÷  $\left[ \right]$  = 60 + 78

**h** 
$$45 +$$
 =  $450 \div 3 = 6 \times$  =  $232 - 82$ 

# Making good progress!



Class..... Date ......

#### Make both sides of an equation equal, where one side contains a missing number

Complete the following by putting the missing numbers in the boxes.

$$- 246 = 356.5 - 78$$



Class..... Date .....

Complete the following by putting the missing numbers in the boxes.

**C** 26 x 24 = 
$$\div$$
 13

$$x \quad 1.5 = 432 \div 18$$

$$\div$$
 5 = 98 x 12

$$\div$$
 3.5 = 3.84 x 25



Name...... Date...... Date......

3 Have a go at these. They may be tricky - look carefully at the operations.

**C** 
$$4.5 \times$$
 **T** =  $1064 - 785$ 

f 
$$742.6 -$$
 =  $36.23 \times 18$ 

$$k$$
 82291 -  $= 1364 \times 56$ 

$$\div$$
 2.7 = 1006 - 824.1



Name ...... Date ...... Date ......

4 Now try these. Think carefully.

$$\mathbf{C}$$
 1352 ÷ 26 = 16 x 3.25 = 36.23 +

**d** 
$$857.3 - 789.3 =$$
  $\div 4.2 = 36.248 + 31.752$ 

e 
$$23.29 + 13.71 = x 18.5 = 240.5 \div 6.5 = -56.64$$

# You're doing well!



# Part 2

Year 6 (and beyond) Expectations

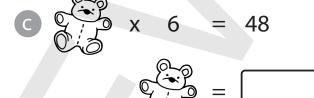
You are now ready to study algebra and practise your skills!



# Begin to use letters to represent variables.

Put the missing numbers in the boxes.





y

 $\boldsymbol{\chi}$ 

- 2 In algebra, instead of symbols to represent numbers, we can use letters.
- 26  $\chi$  $\boldsymbol{\chi}$ 
  - y 24 48  $\chi$
- 27 y 19 y
  - 68 b47 152 42 a b $\boldsymbol{a}$
- b27 62 b

183 127  $\boldsymbol{a}$  $\boldsymbol{a}$ 

92

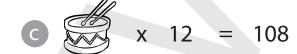
- 3 Now try these.

- **g**  $b \times 8 = 96$  b =
- 4 Have a go at these. Take care the operations are mixed up.

- 9 x a = 108  $a = \boxed{}$

# Begin to use letters to represent variables.

Put the missing numbers in the boxes.



2 In algebra, instead of symbols to represent numbers, we can use letters.

e 
$$487 + y = 726$$
  
 $y =$ 

**b** 
$$232 - y = 87$$
  $y =$ 

**h** 
$$1462 - a = 744$$
  $a = \boxed{}$ 

3 Now try these.

a 
$$x \times 12 = 228$$

$$x =$$

e 17 x 
$$y = 646$$

**b** 
$$195 \div y = 13$$

$$y =$$

**f** 840 
$$\div$$
  $x = 21$ 

$$x =$$

$$9 \times a = 234$$

$$a =$$

g 
$$b \times 24 = 1272$$

**d** 
$$b \div 14 = 53$$

$$b =$$

**h** 
$$a \div 36 = 59$$

$$a =$$

4 Have a go at these. Take care - the operations are mixed up.

a 
$$152 + x = 932$$

$$x =$$

$$y x 36 = 180$$

$$y =$$

**b** 
$$y - 488 = 229$$

$$y =$$

$$x =$$

$$a = 999$$

$$b + 463.2 = 541.8$$

$$b =$$

$$b \div 23 = 831$$

$$b =$$

**h** 
$$2688 \div a = 32$$

$$a =$$

#### Solve equations where letters represent missing numbers.

Remember, in algebra we can use letters to represent missing numbers.

- 1 Find the value of x or y in these equations. Put your answers in the boxes.

- 2 Now find the value of a or b in these.

- 3 Find the value of the letters in these mixed addition and subtraction equations.
- - $x = \boxed{\phantom{a}}$  y 6 = 37

- a 9 = 87 a =
- f 55 + x = 92x =

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- 4 Now try to find a or b in these equations.

- **5** What is the value of x or y?
- a 21  $\div$  y = 7  $y = \boxed{\phantom{a}}$

- 6 Find the value of the letters in these mixed multiplication and division equations.

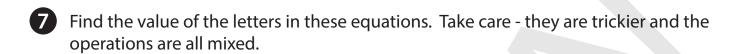
- $8x = 48 \quad (8x \text{ means the same as } 8 \times x)$   $x = \boxed{}$
- 12a = 60  $a = \boxed{ }$

**Clue:** Whatever you do to one side you must do to the other.

**Example:** 4x = 16

To find the value of x, divide both sides by 4.

So x=4



**h** 
$$5x + 123 = 478$$
  $x =$ 

$$y - 57 = 32$$

$$y = \boxed{\phantom{a}}$$

$$6a = 72$$

$$a = \boxed{\phantom{a}}$$

**f)** 6 x 
$$2a = 120$$
  $a = \boxed{}$ 

$$b = \begin{bmatrix} b \\ b \end{bmatrix}$$

$$7 y = 84$$

$$y = \boxed{\phantom{0}}$$

#### Solve equations where letters represent missing numbers.

Remember, in algebra we can use letters to represent missing numbers.

Find the value of x or y in these equations. Put your answers in the boxes.

$$x + 52 = 197$$

$$X =$$

$$y + 126 = 387$$

$$y =$$

**b** 
$$74 + y = 188$$

$$y =$$

d 
$$648 + x = 828$$

$$x =$$

Now find the value of a or b in these.

a 
$$178 - x = 56$$

$$X =$$

$$c$$
 743 -  $y$  = 471

$$y =$$

**b** 
$$y$$
 - 412 = 76

$$d x - 354 = 237$$

$$X =$$

Find the value of the letters in these mixed addition and subtraction equations.

d

a 
$$127 + x = 436$$

$$X =$$

$$y + 382 = 947$$

$$y =$$

b 
$$y$$
 - 284 = 173

$$y =$$

$$e \quad a \quad - \quad 676 = \quad 283$$

$$a =$$

$$b = 628$$

$$f$$
  $x$  + 423 = 1638

$$x =$$

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4 Now try to find a or b in these equations.

a  $a \times 12 = 144$ 

a =

 $b \times 8 = 112$ 

b =

b 11 x b = 143

b =

d 5 x a = 950

a =

**5** What is the value of x or y?

a 238  $\div$  y = 7

y =

 $896 \div x = 8$ 

X =

**b**  $x \div 9 = 74$ 

x =

d  $y \div 13 = 27$ 

y =

6 Find the value of the letters in these mixed multiplication and division equations.

a  $y \div 12 = 79$ 

*y* =

e  $3a \div 27 = 14$ 

a =

b  $9a = 279 (9a \text{ means the same as } 9 \times a)$ 

a =

c 315 ÷ b = 15

b =

12x = 672

X =

**Clue:** Whatever you do to one side you must do to the other.

**Example:** 4x = 16

To find the value of x, divide both sides by 4.

**So** x = 4

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7 Find the value of the letters in these equations. Take care - they are trickier and the operations are all mixed.

a 436 + 
$$x = 843$$
 g 7668 ÷  $2a = 9$   
 $x =$ 

-----

**b** 
$$b \div 52 = 48$$
 **h**  $4x + 637 = 2329$   $b =$ 

**c** y - 158 = 674 **i** 2y - 749 = 873 y =

15
$$a = 840$$
 j 594 ÷ 6 $a = 33$    
  $a =$ 

(e) 426 - b = 178 (k)  $2b \div 46 = 137$  (b) b =

#### Solve equations where letters represent missing lengths.

1 Find the value of x or y in these equations. Put your answers in the boxes.

a 
$$12 \text{cm} + x = 19 \text{cm}$$
  
 $x = \boxed{\qquad \qquad \text{cm}}$ 

$$b + 12km = 84km$$

$$b = km$$

2 Now find the missing lengths in these multiplication or division equations.

a 
$$8 \text{km}$$
 x  $y = 48 \text{km}$   $y = \frac{1}{2} \text{km}$ 

$$x \div 5m = 15m$$

$$x = \boxed{m}$$

b 
$$48 \text{cm} \div a = 4 \text{cm}$$

$$a = \boxed{\text{cm}}$$

3 What are the missing lengths?

a 
$$82m - x = 21m$$

$$x = \boxed{\qquad m}$$

$$y \quad x \quad 12cm = 96cm$$

$$y = cm$$

#### Solve equations where letters represent missing lengths.

1 What are the missing lengths? Put your answers in the boxes.

a 
$$72cm + x = 196cm$$

$$X =$$
 cm

$$\bigcirc$$
 378mm -  $y = 158$ mm

$$y =$$
 mm

**b** 
$$a - 72cm = 123m$$

$$a =$$
 m

$$b + 426 \text{km} = 513 \text{km}$$

$$b = \boxed{\phantom{a}}$$
 km

2 Now find the missing lengths in these multiplication or division equations.

a 
$$7 \text{km} \times y = 735 \text{km}$$

$$y = km$$

$$c 338m \div x = 26m$$

$$b \quad a \div \quad 8_{\text{cm}} \quad = \quad 54_{\text{cm}}$$

$$a = \int_{\text{cm}}$$

$$b \times 46 \text{mm} = 736 \text{mm}$$

$$b = \boxed{\phantom{a}}$$

3 What are the missing lengths?

a 
$$552m - x = 327m$$

$$X =$$
 m

**d** 
$$4b \div 72m = 432m$$

$$b =$$
 m

b 
$$413 \text{km} + a = 1623 \text{km}$$

$$a = \begin{bmatrix} km \end{bmatrix}$$

$$e 2x + 14.34$$
cm =  $28.54$ cm

$$X =$$
 cm

 $y \times 17cm = 595cm$ 

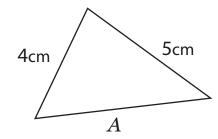
$$y =$$
 cm

(f) 
$$5y \times 3.2m = 112m$$

$$y = \int_{m}^{\infty}$$

#### Solve equations where letters represent missing lengths in shapes.

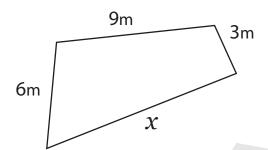
1 Look at the triangle below. Use the equation shown to find the length of side A.



$$4cm + 5cm + A = 15cm$$

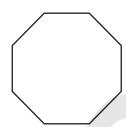
$$A = \boxed{\qquad cm}$$

2 What is the length of the missing side in April's garden?



$$28m = x + 9m + 3m + 6m$$
 $= x$ 

 ${\bf 3}$  y centimetres represents the length of each side of a regular octagon. The perimeter of the octagon is 24mm.



**so** 
$$8y = 24mm$$

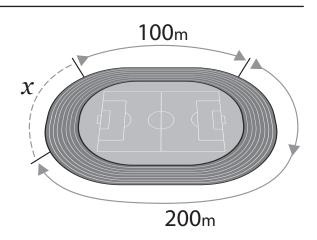
(8y means the same as 8 x y)

$$y =$$
 mm

4 Look at the track. Use the equation to find the length of *x*.

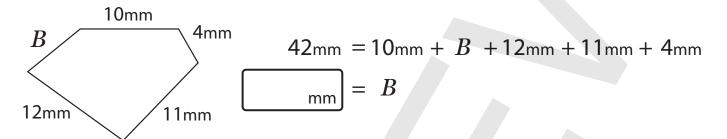
$$400m = 100m + x + 200m$$

$$= x$$

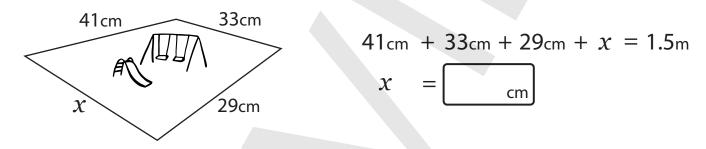


#### Solve equations where letters represent missing lengths in shapes.

1 Look at the shape below. Use the equation shown to find the length of side B.



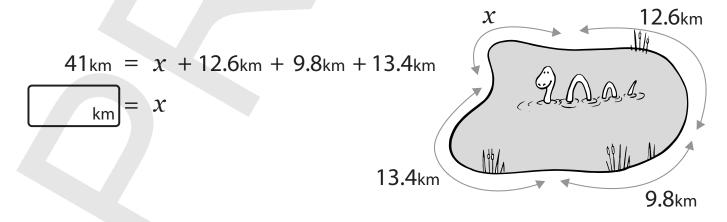
What is the length of the missing side in the model playground below? Look carefully at the measurements.



The perimeter of a regular nonagon-shaped lawn is 40.5 metres. The length of each side of the lawn is represented by  $\boldsymbol{y}$  metres.

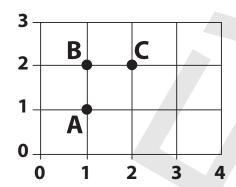
so 
$$9y = 40.5 \text{m}$$
 (9y means the same as  $9 \times y$ )
$$y = \boxed{\text{m}}$$

4 Look at the lake. Use the equation to find the length of x.



### Solve equations where letters represent missing co-ordinates..

Look at the co-ordinate grid and use it to answer the questions below.





The co-ordinates of  $\mathbf{A}$  are (1,1). What are the co-ordinates of **C**?

Shape **ABCD** is a square. What are the co-ordinates of **D**?

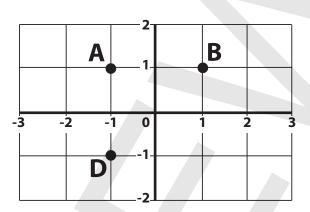
**F** is exactly the same distance from **C** as is **B**. What is the missing co-ordinate?

Shape **ABFG** is a rectangle. What are the co-ordinates of **G**?

If lines were drawn on the grid to make shape **ABG**, what would the shape be?

2 Look at the co-ordinate grid and use it to answer the questions below.





a What are the co-ordinates of **A** and **B**?

B = ( .....)

b Shape **ABCD** is a square. What are the co-ordinates of **C**?

The triangle **ADF** is drawn on the grid. What could the missing co-ordinates be?

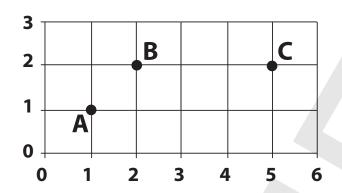
$$\mathbf{F} = (2, \dots, )$$

or 
$$F = (2, ....)$$

or 
$$F = (2, ...)$$

# Solve equations where letters represent missing co-ordinates..

Look at the co-ordinate grid and use it to answer the questions below.





a What are the co-ordinates of A, B and C?

$$A = ( , )$$

**ABCD** is a parallelogram. What are the co-ordinates of **D**?

Line **BF** is perpendicular to the x-axis. What is the missing co-ordinate for point **F**?

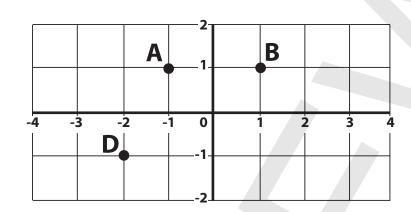
A line parallel to **AB** is drawn on the grid. The co-ordinates of one end of the line are (2, 0). What could the co-ordinates of the other end be (point **G**)?

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Look at the co-ordinate grid and use it to answer the questions below.







What are the co-ordinates of **A**, **B** and **D**?

$$\mathsf{B} = ( \ \ , \ \ )$$

Shape **ABCD** is a trapezium. What are the co-ordinates of **C** if it is the same distance from the u axis as **D**?

The rectangle **ABEF** is drawn on the grid. Side **BE** is parallel to the y-axis. What could the co-ordinates of **E** and **F** be?

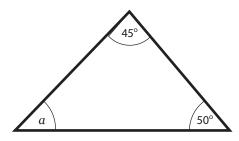
$$F = ($$

$$F = ($$

$$F = ( , )$$

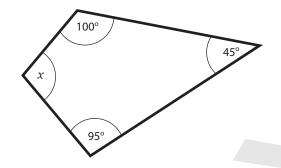
# Solve equations where letters represent missing angles.

1 Use the equation to find the size of angle a.

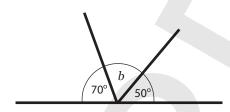


$$45^{\circ} + 50^{\circ} + a = 180^{\circ}$$
 $a = 6^{\circ}$ 

2 Find angle x in this shape.



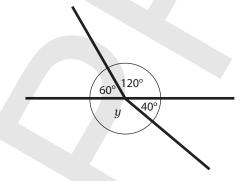
3 Find angle b.



$$70^{\circ} + 50^{\circ} + b = 180^{\circ}$$

$$b = \boxed{\phantom{a}^{\circ}}$$

4 Find angle y.

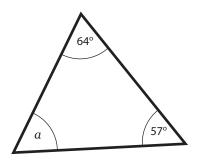


$$120^{\circ} + 40^{\circ} + y + 60^{\circ} = 360^{\circ}$$

$$y = \boxed{\phantom{0}^{\circ}}$$

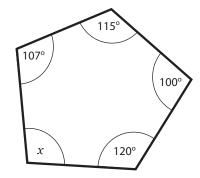
#### Solve equations where letters represent missing angles.

1 Use the equation to find the size of angle a.

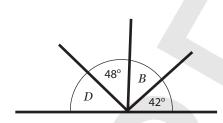


$$64^{\circ} + 57^{\circ} + a = 180^{\circ}$$
 $a = 64^{\circ}$ 

**2** Find x in this shape.



3 Angle B, and angle D are equivalent. What is angle B?

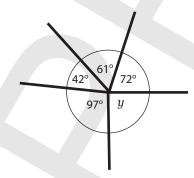


$$D = B$$

$$D + 48^{\circ} + 42^{\circ} + B = 180^{\circ}$$

$$B = \boxed{\phantom{A}^{\circ}}$$

4 How many degrees is angle *y*?



#### Use simple formulae.

Use the formula below to find the area of the following rectangles.

A (Area) = l (length) x w (width)

- = 3cm
- 6m
- l = 10 mm

- = 43 cm $\boldsymbol{w}$
- 9<sub>m</sub> $\boldsymbol{w}$

=46mm

- $\,{\rm cm}^2$  $\boldsymbol{A}$
- $m^2$  $\boldsymbol{A}$
- $\,\mathrm{mm}^2$
- Now use the formula to find the missing width or length.
- 8cm
- 15cm

- cm
- 9<sub>m</sub> w

wcm

- $= 24 cm^2$
- $63 \text{m}^2$

- $= 30 cm^2$
- Use the formula below to find the missing values in the table.

V (Volume) = (l) length x (w) width x (h) height

	l	w	h	V
Cuboid A	3cm	2cm	1cm	cm <sup>3</sup>
Cuboid B	5m	m	4m	20m <sup>3</sup>
Cuboid C	3 <sub>mm</sub>	2 <sub>mm</sub>	mm	36mm <sup>3</sup>
Cuboid D	cm	2cm	10cm	60cm <sup>3</sup>

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The formula for the area of a parallelogram is A = b (base) x h. Use this to complete the table below.

	A	b	h
Parallelogram A	16cm <sup>2</sup>	4cm	cm
Parallelogram B	$m^2$	8m	бm
Parallelogram C	54mm <sup>2</sup>	mm	бmm

Use the formula below to find the missing values in the table below.

$$A = \frac{b \times h}{2} \text{ or } \frac{1}{2} \times b \times h$$

	A	b	h
Triangle A	$cm^2$	7cm	2cm
Triangle B	6cm²	3cm	cm
Triangle C	10m <sup>2</sup>	m	5m



6 In the formula D = 2r, D represents the diameter of a circle and r represents the radius. Use the formula to find the missing values.

	D	r
Circle A	cm	4cm
Circle B	12m	m
Circle C	24cm	cm
Circle D	m	13m

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# **ANGLE FACT BOX**

Fact	Equation
The sum of the interior angles of a triangle is 180°	$a+b+c=180^{\circ}$
The sum of the interior angles of a quadrilateral is 360°	$a + b + c + d = 360^{\circ}$
The sum of the interior angles of a pentagon is 540°	$a+b+c+d+e=540^{\circ}$

7 Use the equations shown in the fact box above to find the missing values.

Shape	Angle A	Angle B	Angle C	Angle D	Angle E
Triangle	64°	72°	O		
Quadrilateral	75°	95°	105°	0	
Square	0	o	0	0	
Pentagon	110°	100°	90°	0	140°
Regular Pentagon	0	108°	0	0	0



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# Use simple formulae.

Use the formula below to find the area of the following rectangles.

A (Area) = l (length) x h (height)

$$a l = 13$$
cm

**b** 
$$l = 27m$$

$$c$$
  $l$  = 23mm

$$w = 8cm$$

$$w = 9m$$

$$w = 13$$
mm

$$A = \left[ \begin{array}{cc} & & \\ & \text{cm}^2 \end{array} \right]$$

$$A = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}$$

$$A = \frac{1}{\text{mm}^2}$$

Now use the formula to find the missing width or length.

$$a l = 14 cm$$

$$cl = 24cm$$

$$w =$$
 cm

$$w = 16m$$

$$w =$$
 cm

$$A = 98 cm^2$$

$$A = 672 \text{m}^2$$

$$A = 504 \text{cm}^2$$

Use the formula below to find the missing values in the table.

V (Volume) = (l) length x (w) width x (h) height

	l	w	h	V
Cuboid A	4cm	cm	7cm	<b>56</b> cm <sup>3</sup>
Cuboid B	8m	6m	9m	m <sup>3</sup>
Cuboid C	4.5mm	2 <sub>mm</sub>	mm	108mm <sup>3</sup>
Cuboid D	cm	4cm	7cm	252cm <sup>3</sup>

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The formula for the area of a parallelogram is A = b (base) x h. Use this to complete the table below.

	A	b	h
Parallelogram A	156cm <sup>2</sup>	12cm	cm
Parallelogram B	$m^2$	15m	16m
Parallelogram C	374mm <sup>2</sup>	22 <sub>mm</sub>	mm

Use the formula below to find the missing values in the table below.

$$A = \frac{b \times h}{2} \text{ or } \frac{1}{2} \times b \times h$$

	A	b	h
Triangle A	$cm^2$	8cm	29cm
Triangle B	300cm <sup>2</sup>	5cm	cm
Triangle C	496m <sup>2</sup>	m	16m



6 In the formula D = 2r,  ${\cal D}$  represents the diameter of a circle and r represents the radius. Use the formula to find the missing values.

	D	r
Circle A	m	57m
Circle B	1240cm	cm
Circle C	265m	m
Circle D	cm	7.25cm

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# **ANGLE FACT BOX**

Fact	Equation
The sum of the interior angles of a triangle is 180°	$a+b+c=180^{\circ}$
The sum of the interior angles of a quadrilateral is 360°	$a + b + c + d = 360^{\circ}$
The sum of the interior angles of a pentagon is 540°	$a+b+c+d+e=540^{\circ}$

7 Use the equations shown in the fact box above to find the missing values.

Shape	Angle A	Angle B	Angle C	Angle D	Angle E
Triangle	62.5°	78°	0		
Equilateral Triangle	0	0	0		
Square	0	0	0	0	
Pentagon	116°	104.5°	87.5°	0	141°
Regular Pentagon	0	0	0	0	0



Look at the formula. n represents the number of sides.

 $(n-2) \times 180^{\circ} = \text{sum of the interior angles of any polygon}$ 

8 Use this formula to complete the missing values in the polygons below.

	Number of sides (name of shape)	Sum of interior angles	Each interior angle of the regular polygon
a	9 (nonagon)		0
b	10 (decagon)	°	0
C		1080°	°

d Now use the formula to find the missing angle in the irregular hexagon below.

Angle A = 
$$115^{\circ}$$

Angle B = 
$$127^{\circ}$$

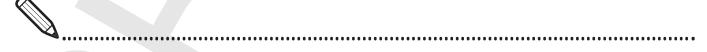
Angle C = 
$$120^{\circ}$$

Angle D = 
$$131^{\circ}$$

Angle E = 
$$112^{\circ}$$

Angle 
$$F = \bigcirc$$

e Write down a possible combination for the angles in a pentagon (5 sides).



Well done!



Na	me	••••••	•••••	Class	••••••••	Date	••••••
Ge	enerate a	ınd describ	e linear nur	mber seq	uences.		
0		number sequ ng numbers.	ience below, f	ind the ru	e to describe	the pattern	and write
EXA	<b>MPLE</b> 4,	8,	12,	16,	20	24	28
	add	4					
a	9,	14,	19,	24,			
<b>b</b>	45,	54,		72,		90,	
	78	67,		45,	34		
<b>d</b>	5,	2,	-1,	-4,			
e	125,		75,	50,		0,	

Nar	ne	•••••	•••••	Class	•••••••	Date	••••••••••••
2	Now try the:	se. <b>Clue</b> - the	pattern is	n't just addin	ng or subtra	cting.	
a	2,	4,	8,		32,		
	1		••••				
b	1,	4,	16,	64,			
	1						
С	729,	243,		27,	9,		
	<u> </u>	, _					
d	220	160	00		20		
	320,	160,	80,		20,		
V	3	••••••					
e	0.04,	0.2,	1,	5,			
		•••••	••••••••	••••••	•••••••	••••••	•••••••••••••••••••••••••••••••••••••••
f	1.25,	2.5,	5,	10,			
	1	••••••	•••••	•••••		•••••	••••••

Name	•••••	•••••	C	lass	••••••	Date	
3 For	-		o find the pat	ttern in	the difference l		numbers.
·	2,	3,	5,	8,	12	17	23
	ncrease	decrease d	lifference by	1 2	and add sul	btract	
a	8,	10,	13,	17,			
i	ncrease	<b>decrease</b> d	lifference by	1   2	and <b>add su</b> l	otract	
<b>b</b> 2	25,	24,	22,	19,			
i	ncrease	decrease d	lifference by	1   2	and <b>add</b> sul	btract	•••••
C	2,	12,	21,	29,			
<b>l</b> i	ncrease	<b>decrease</b> d	lifference by	1   2	and <b>add su</b> l	btract	
4 No	ow have a g	go at writing	the full rule a	and find	ding the missing	g numbers.	
a	1,	2,	5,	10,			
i	ncrease	<b>decrease</b> d	lifference by	1   2	and <b>add   su</b> l	otract	•••••
<b>b</b> 5	50,	40,	31,	23,			
O.i.	ncrease	decrease d	lifference by	1   2	and <b>add   su</b> l	btract	·····

Nar	me	•••••	• • • • • • • • • • • • • • • •	Cla	SS	••••••	Date	••••••
5	Describe	how these	numbers a	ire special	and com	plete the s	equence.	
a	1,	4,	9,			25,		
	λ							
	ა	······································	7		12	1.7		<u> </u>
<b>b</b>	2,	3,	/,		13,	17,		
	<b>3</b>	•••••	•••••	•••••				••••••
6	These are	e tricky! The	ere are two	rules.				
EXAI	<b>MPLE</b> +3	-2	+3	-2		+3	-2	+3
2,			3,	6,	4,	7	5	8
								J
	aaa	3, sul	otract	<b>2</b>				
a	4,	5,	3,	4,	2,			
	λ							
~	<b>4</b>							
			•••••••••••	•••••				
b	3,	8,	12,	17,	21,			)
<b>b</b>	3,	8,	12,	17,	21,			
<b>b</b>	<b>3</b>			•••••	••••••			)
<b>D</b>	<b>3</b>	20,		•••••	••••••			
<b>D</b>	<b>3</b>			•••••	••••••			

me	••••••	• • • • • • • • • • • • • • • • • • • •	Class	•••••	Date	• • • • • • • • • • • • •
nerate ar	nd descri	be linear nui	mber seq	uences.		
			ind the rul	e to describe th	ne pattern a	and write
<b>MPLE</b> 8,	14,	20,	26,	32	38	44
	6					
61,	68,		82,			
128,		106,	95,			
17,	20,		2	9,	35,	
	-3,	0,		9,	12,	
65,		3.	5,		5,	
	For each n the missin WPLE 8, add 17,	For each number sectifie missing numbers  WPLE  8, 14,  add 6  17, 68,  17, 20,  -3,	For each number sequence below, fithe missing numbers.  WPLE  8, 14, 20,  add 6  61, 68,  128, 106,  17, 20,	To each number sequence below, find the rul the missing numbers.  WPLE  8, 14, 20, 26,  add 6  61, 68, 82,  128, 106, 95,  17, 20, 26	nerate and describe linear number sequences.  For each number sequence below, find the rule to describe to the missing numbers.  MPLE  8, 14, 20, 26, 32  add 6  61, 68, 82, 128, 106, 95, 17, 20, 29, 29, 34  17, 20, 9, 9, 9, 34	nerate and describe linear number sequences.  For each number sequence below, find the rule to describe the pattern at the missing numbers.  WPLE  8, 14, 20, 26, 32 38  add 6  61, 68, 82,

Name	<u>,</u>	•••••	•••••	. Class	••••••	Date	•••••••••••••••••••••••••••••••••••••••
<b>2</b> No	ow try th	ese. <b>Clue</b>	- the pattern	isn't just add	ing or subtra	cting.	
a	4,			32,		128,	
<b>.</b>		•••••					
b	8,		72,	216,		1944	
<b>C</b> 1	76,		44,		11,	5.5,	
	7 0,		,		,	3.37	
٧.	•••••						
<b>d</b> 0	.25,		1,		4,		
<b>W</b> .	••••				••••••	••••••	•••••••
e	48,		12,			1.5	
				•••••••	•••••••	••••••	••••••
f			2,		0.5,	0.25,	
		•••••				•••••	••••••

For these, you will need to find the pattern in the difference between the number 24, 25, 27, 30, 34 39 45 increase   decrease difference by 1 2 3 and add subtract	
24, 25, 27, 30, 34 39 45	ers.
increase   decrease difference by 1 2   3 and add subtract	
	••••
a 56, 53, 50, 35,	
increase   decrease difference by 1   2   3 and add   subtract	••••
<b>b</b> 5, 15, 24,	
increase   decrease difference by 1   2   3 and add   subtract	••••
4 Now have a go at writing the full rule and finding the missing numbers.	
a 11, 10, 5, — -4, —	
increase   decrease difference by 1   2   3 and add   subtract	••••
<b>b</b> 40, 33, 27, 22,	
increase   decrease difference by 1   2   3 and add   subtract	••••
3, 1, -2,	
increase   decrease difference by 1   2   3 and add   subtract	•••••

Name Class	. Date
5 Describe how these numbers are special and complete the	e sequence.
a 4, 16,	49,
<b>b</b> 37	
6 These are tricky! There are two rules.	
<b>EXAMPLE</b> +4 -5 +4 -5 +4	-4 -5
16 20 15 19 14	18 13
add 4, subtract 5	•••••••••••••••••••••••••••••••••••••••
a 13, 17, 9, 5,	5,
<b>b</b> 8, 16, 14, 28,	
8, 10, 14, 28,	
<b>C</b> 5, 15, 17, 53,	

## Use a formula to generate a number in a number sequence.

1 The formula for the sequence below is:

 $(n \times 3) + 1 \qquad (n = 1^{st}, 2^{nd}, 3^{rd}, 4^{th} \text{ number etc})$ 

4 7 10 13 16 1<sup>st</sup> 2<sup>nd</sup> 3<sup>rd</sup> 4<sup>th</sup> 5<sup>th</sup>

Use the formula to find the missing numbers in the sequence.

#### **EXAMPLE**

 $8^{th}$   $\longrightarrow$   $(8 \times 3) + 1 = 25$ 

a 5<sup>th</sup> → d 10<sup>th</sup> →

**6** 9<sup>th</sup> →

2 Now use the formula  $(n \times 5) + 3$  to fnd the missing numbers.

a  $1^{st} \longrightarrow \boxed{ d 8^{th} \longrightarrow } \boxed{ }$ 

**b** 3<sup>rd</sup> → **e** 10<sup>th</sup> →

**C** 5<sup>th</sup> → **f** 14<sup>th</sup> →



You're doing a great job!

Name	Class	Date

# Use a formula to generate a number in a number sequence.

The formula for the sequence 10, 17, 24, 31 is  $(n \times 7) + 3$ , where n represents the 1<sup>st</sup>, 2<sup>nd</sup>, 3<sup>rd</sup> number etc.

Use the formula to find the missing numbers in the sequence.

#### **EXAMPLE**

$$8^{th} \longrightarrow (8 \times 7) + 3 = 59$$

- a 12<sup>th</sup>→
  b 15<sup>th</sup>→
- 2 Now use the formula  $n^2 \times 2$
- a 1<sup>st</sup> →
- **b** 7<sup>th</sup> →
- 3 Have a go at using the formula  $n^3 8$
- a 4<sup>th</sup> →
- 4 Write the first 5 numbers in the sequence using the formula  $(n \times 9) 20$

## Express missing number problems algebraically.

- 1 Complete the following.
- Jaz had 16 precious coins. He gave x coins to Afzal. He had 7 left. **Circle** the equation which would show how many precious coins Jaz gave to Afzal.

$$16 \div x = 7$$

$$16 \div x = 7$$
  $16 - x = 7$ 

$$16 + 7 = x$$

David bought 8 packets of biscuits. Each packet had the same number of biscuits. There were 208 biscuits altogether. **Circle** the equation which could be used to work out how many biscuits were in each packet (y).



$$y = 8 \times 208$$

$$y = 208 - 8$$

$$y = 208 \div 8$$

There are 18 tennis balls in the bag. 7 are green and x are orange. **Circle** the equation which could be used to find *x*.

$$x - 18 = 7$$

$$18 = 7 + x$$

$$x = 7 - 18$$



Molly has £4. She spends £y at the shop. She has £1.50 left. **Circle** the equation which could be used to find y.

$$fy = f4 - f1.50$$
  $f1.50 + f4 = fy$   $f4 = f1.50 - fy$ 

£1.50 + £4 = £
$$y$$

$$£4 = £1.50 - £y$$

Na	me	Class	Date
2	Write down a suitable equation you Then solve them.	ı could use to solve the p	oroblems.
a	A toy shop had 8 toy garages. Each How many cars were there altogeth		
	<i>a</i> =	a =	
b	A wall had 48 bricks. There were 23 new bricks $(b)$ were used in the wall		vere new. How many
	$b = \square$	<i>b</i> =	
C	The Crafty Cake Shop sells 4 birthda as many. How many birthday cakes	•	•
	$x = \Box$	<i>X</i> =	=
d	Holly buys 27 sweets. Harry buys 1/3 a	as many. How many swe	ets does Harry buy (s)?
	$s = \square$	S =	
		\$ 5 S	

# Express missing number problems algebraically.

- 1 Complete the following.
- A bag contains x nails. Charlie used 56 to build a cabinet. There were 127 nails left in the bag. **Circle** the equation which could be used to work out how many nails were in the bag to start with.

$$x = 127 - 56$$

$$x = 56 + 127$$

$$x = 56 \times 127$$



Gerry put the buns he had made into 14 tins. He had made 252 buns. Circle the equation which could be used to work out how many buns were in each tin (y).

$$14 + 252 = y$$

$$252 \times 14 = y$$

$$252 \div 14 = y$$

Four friends went to a football match. They each paid £4.50 for a drink and a burger. **Circle** the equation which could be used to work out the total bill (b).

$$£4.50 + 4 = b$$

£4.50 
$$\div$$
 4 =  $b$ 

£4.50 
$$\div$$
 4 = b £4.50  $\times$  4 = b

On Saturday 1364 people visited the Green Garden Centre. On Sunday 956 people visited. Circle the equation which could be used to work out how many people visited the garden centre altogether on Saturday and Sunday (a).

$$1364 + 956 = a$$

$$1364 - 956 = a$$

$$1364 \div a = 956$$

Name	Class	Date

- Write down a suitable equation you could use to solve the problems. Then solve them.
- 1486 people attend the Laid Back Leisure Centre over one weekend. 652 are female. How many are male (a)?



$$a =$$

There were three times as many tiles in the large pool as in the small pool. The small pool had 876 tiles. How many tiles were in the large pool (b)?

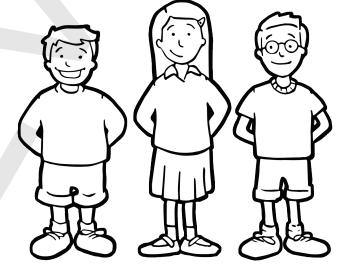
b =		

$$b =$$

Mrs Shah shared £24.45 evenly between her three children. How much did they each get (x)?







Megan spent £2.64 on a necklace, £1.25 on some sweets and £15.72 on a present for her mum. How much did she spend altogether (y)? Write the full equation on the line.

.....

$$y = f$$

# Solve equivalent expressions, where a letter represents one unknown number.

1 Find the missing numbers in the following.

$$4y = 16 \times 2$$

$$y = \boxed{\phantom{a}}$$

**b** 
$$38 - 9 = y - 3$$
  $y =$ 

**f** 
$$4 + 23 = a + 21$$
  $a =$ 

$$6a = 3 \times 12$$

$$a = \boxed{\phantom{a}}$$

- 2 Now try these.
- a 15 + x = 24 6x =
- **b** 8 x 7 = 112 ÷ y y =

**3** Have a go at these - look carefully at the operations.

a 
$$14 + y = 3 \times 6$$
  
 $y =$ 

$$8x = 49 + 39$$
$$x = \boxed{ }$$

**b** 
$$27 \div 9 = 52 - x$$
  $x =$ 

f 84 - 
$$a = 17 \times 3$$
 $a =$ 

$$8b = 33 - 9$$

$$b = \boxed{\phantom{a}}$$

**9** 
$$288 \div y = 181 - 37$$
  $y =$ 

d 15 + 25 = 
$$a$$
 - 2  $a$  =

4 Now try these. Think carefully - they are tricky!

a 
$$122 + 22 = 4y = 217 - 73$$
  
 $y =$ 

**b** 
$$156 - a = 243 \div 3 = 3 \times 27$$
 $a = \boxed{ }$ 

**d** 
$$206.5 + 0.5 = b \div 3 = 571 - 364$$

$$b = \boxed{}$$

## Solve equivalent expressions, where a letter represents one unknown number.

1 Find the missing numbers in the following.

$$91y = 26 \times 7$$

$$y = \boxed{}$$

**b** 
$$169 - 43 = y - 42$$
  $y =$ 

f 
$$178 + 105 = a + 94$$
  
 $a =$ 

$$a = \begin{bmatrix} 12 & x & 9 \\ a & = \end{bmatrix}$$

9 416 ÷ 
$$x = 128 \div 16$$
  
 $x =$ 

d 
$$182 \div b = 156 \div 12$$
  
 $b =$ 

- 2 Now try these.
- a 2917 + x = 4613 1212x =
- e 9427 649 = y + 689y =
- **b** 56 x 73 =  $y \div 7$   $y = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$
- **f**  $a \div 23 = 3.5 \times 16$   $a = \boxed{}$
- $\begin{array}{c} \mathbf{C} & 9210 x = 4164 + 2857 \\ x = \boxed{\phantom{0}} \end{array}$
- g 9473 1849 = x + 3476x =
- **d**  $1125 \div 25 = 18b$  b =
- **h**  $2.5b = 520.8 \div 8.4$   $b = \boxed{}$

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3 Have a go at these - look carefully at the operations.

a  $67 + y = 12 \times 13$ y =

e 58x = 769 + 159x =

**b**  $350 \div 14 = 113 - x$ x =

f  $6842 - a = 36 \times 53$  a = 6

b = 60 b = 60

d 1026 + 3728 = 7214 - a a =

- **h**  $1512 \div 27 = 39.14 + b$  b =
- 4 Now try these. Think carefully they are tricky!

a  $362.6 + 158.4 = 1042 \div y = 1341 - 820$ y =

3478  $\div$  37 = 37.6 x 2.5 = 8.764 + x

**d**  $74.7 + 18.2 = b \div 4.2 = 1714 - 1621.1$  b =

# Find pairs of numbers that satisfy an equation with two unknowns.

- 1 For each of the following, find the value of  $\triangle$  . Clue find the value of the other shapes first.

- 2 Solve the following. **Clue** one letter is easy to work out, so find that first.
- x = 26 + 14 x = y + y x =
- a = 97 76  $a = b \div 3$   $b = \square$
- **b**  $y = 8 \times 8$  y = 73 a a =
- 63 + 14 = y 85 x = y  $x = \boxed{}$
- $b = 99 \div 11$  b = 6 + x  $x = \square$

- 3 Have a go at solving these.
- 17 + a =21 b = 2a*b* =

- C 10*b* 80 = = b + 31 $\boldsymbol{\chi}$  $\boldsymbol{\chi}$
- 56 ÷  $\boldsymbol{\chi}$  $\boldsymbol{\chi}$ y + yy
- 16 = y a + y =41  $\boldsymbol{a}$
- 4 Try these they are getting even trickier!
- 27  $\div a =$  $+ 2 = 44 \div b$ a b
- x + 38 = 442x = y - 9y =
- b 14 - y =20 + y = 31 $\chi$ X =
- e b - 15 = 354a = b - 18a

2*b* 30 -b =*2y* 27 y

3y =60  $x \div 2$ y - 9 =  $\chi =$ 

Have a go at these. You will need to think very carefully!

$$4x = 24 \div 2$$

$$22 + x = 30 - y$$

$$y = \boxed{}$$

$$y - 14 = 3 \times 2$$

$$y \div 4 = 1 + x$$

$$x = \boxed{ }$$

- 6 These are very challenging! Try them.
- a x + 4 = 4 + 11 + 5  $x \div 2 = 2 + a$ a =

 $a + 7 = 3 \times 9$  y = a + a + 4  $y = \boxed{}$ 

**b**  $4 + y + 3 = 8 \times 2$  60 + x = 7y $x = \Box$ 

# Find pairs of numbers that satisfy an equation with two unknowns.

- 1 For each of the following, find the value of  $\triangle$  . Clue find the value of the other shapes first.
- a = 179 23

= 119 + 
$$\triangle$$

- $\begin{array}{ccc}
  \text{d} & \bigcirc & = & 156 & 68 \\
  & \bigcirc & = & 124 \triangle \\
  & \triangle & = & \boxed{}
  \end{array}$
- 2 Solve the following. **Clue** one letter is easy to work out, so find that first.
- x = 127 + 43

$$x = y + y$$

$$y =$$

 $d \quad a = 314 - 179$ 

$$a = b \div 8$$

$$b =$$

b  $y = 13 \times 13$ 

$$y = 204 - a$$

e 474 + 383 = y

$$1068 - x = y$$

 $b = 350 \div 14$ 

$$b = x^2$$

$$X =$$

 $b = 36 \times 14$ 

$$b = 1008 \div y$$

$$y =$$



- 3 Have a go at solving these.
- $a \quad 156 + a = 242$  b = 7a  $b = \boxed{}$
- 26b = 650 x = b + 987  $x = \boxed{}$
- **d** y 176 = 243 a + y = 736a =
- 4 Try these they are getting even trickier!
- $a \quad 516 \div a = 12$   $a \quad + \quad 7 = 250 \div b$   $b = \boxed{}$
- 13x = y 63  $y = \boxed{}$
- **b** 407 y = 392  $y^{2} = 307 x$   $x = \boxed{}$
- e b 843 = 1069 23a = b - 1843a =
- 18b = 306 173 b = 12y  $y = \boxed{}$
- $\begin{array}{rcl}
  \mathbf{f} & 14y &=& 1022 \\
  y & -& 59 &=& x \div 27 \\
  x & = \boxed{\phantom{a}}
  \end{array}$

Have a go at these. You will need to think very carefully!

12
$$x = 420 \div 5$$
  
426 +  $x = 531 - y$   
 $y =$ 

- **b**  $154 \div a = 4 + 7$ 26a = 578 - b $b = \boxed{}$
- e x + 159 = 77 + 108  $y \div 8 = 17x$ y =

- 6 These are very challenging! Try them.
- x + 327 = 136 + 258 + 89  $x \div 12 = 7.5 + a$   $a = \boxed{ }$
- $a + 326 = 17 \times 26$  y = a + a + 76  $y = \boxed{}$
- **b**  $68 + y + 75 = 51 \times 4$  317 + x = 9yx =

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# Enumerate the possibilities of two variables.

1 Look at each of the equations below. Find 3 different pairs of values for a and b.

a  $a \times b = 24$ 

 $\left[ x \right] = 24$ 

x = 24

x = 24

e  $a \times b = 36$ 

| x | = 36

| x | = 36

x = 36

 $b \quad a \quad \div \quad b \quad = 8$ 

| ÷ | = 8

÷ = 8

a + b = 30

| + | = 30

| + | = 30

| + | = 30

a + b = 26

|+ | = 26

| + | = 26

+ = 26

a - b = 6

|-| = 6

|-| = 6

|-| = 6

a - b = 4

= 4

|-| = 4

|-| = 4

 $\mathbf{h} \quad a \quad \div \quad b \quad = 10$ 

| ÷ | = 10

| ÷ | = 10

 $\left| \div \right| = 10$ 

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For these, find the different values of x and y.

= 28 $\chi$ Χ y

Χ = 28

= 28X

Χ = 28

= 27 y  $\chi$ 

= 27

= 27

+= 27

b 40 y  $\chi$  $\boldsymbol{\mathsf{X}}$ 

40 Χ

40 Χ

Χ 40

Χ 40

9  $\chi$ y

9

9

9

9

2  $\chi$ ÷ y

y

2 ÷ y

2 y

2 y

+

d 16 3  $\chi$ + = +

y

3 16 +

3

3 16 +



16

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3	Try these.		
a	There are 6 sweets in a bag. Some a $c+s=6$ and list all the possible cor	-	
b	xy = 12. In the space below, list all tare whole numbers).	he possible combination	as of $x$ and $y$ ( $x$ and $y$
			<del></del> -
C	There were 30 children at a party. There were 30 children at a party. The fewer than 16, and the number of $g$ the equation $b+g=30$ to find all the	irls was greater than 14 a	nd fewer than 21. Use
			<del></del>

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# Enumerate the possibilities of two variables.

Look at each of the equations below. Find 3 different pairs of values for a and b.

a b = 96  $\boldsymbol{a}$ Χ

Χ = 96

Χ = 96

Χ = 96

b = 110X a

X = 110

= 110X

Χ = 110

b b= 12÷  $\boldsymbol{a}$ 

= 12

÷ = 12

= 12

f b= 155+  $\boldsymbol{a}$ 

+= 155

+= 155

+= 155

C b= 77  $\boldsymbol{a}$ +

> += 77

> += 77

> = 77 +

g b= 39 $\boldsymbol{a}$ 

= 39

= 39

= 39

d b= 17 $\boldsymbol{a}$ 

= 17

= 17

= 17

h b13 ÷  $\boldsymbol{a}$ 

= 13

÷ = 13

= 13

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For these, find the different values of x and y.

= 253 = 156 Χ y e + y  $\chi$  $\boldsymbol{\chi}$ = 156 Χ = 253 +

= 156 + = 253 X

= 253 = 156 X +

b = 250= 127y  $\chi$ X  $\chi$ + y

= 250= 127 X +

Χ = 250= 127+

Χ = 250+= 127

= 250Χ += 127

C 25  $\chi$ ÷ y

25

÷ 25

= 25 ÷

25 ÷

d 57 94  $\boldsymbol{\chi}$ + y +

+57 + 94

+57 94

57 94



Na	me Date Date
3	Try these.
a	There were 16 biscuits in a packet. Some were plain $(p)$ and some were chocolate $(c)$ . There were less than 8 chocolate biscuits. Use the equation $p+c=16$ and list all the possible combinations of plain and chocolate biscuits.
b	xy = 20. In the space below, list all the possible combinations of $x$ and $y$ ( $x$ and $y$ are whole numbers).
C	There were 40 children at the youth club. The number of boys ( $b$ ) was greater than 19 and fewer than 26 and the number of girls ( $g$ ) was greater than 14 and fewer than 21. Use the equation $g + b = 40$ to list all the possible combinations of boys and girls.

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## Solve equations using the correct order of operations.

To make sure we carry out calculations in the correct order we use **BODMAS**.

means the same e.g. - squares)

brackets

2(3+4)

as  $2 \times (3 + 4)$ 

order (or other things

division

multiplication addition

a

 $\boldsymbol{a}$ 

52

 $\boldsymbol{\chi}$ 

subtraction

14 - (8 + 3)

 $7 \times 4 + 3$ 

 $-42 \div 7 = x$ 

- Use **BODMAS** to find the missing numbers in these equations.
- (8 + 2) + 3 $\boldsymbol{\chi}$
- b  $15 \div (1 + 2)$ y y
- 4 + 6x 8  $\boldsymbol{a}$  $\boldsymbol{a}$
- 2 d 30 ÷  $\boldsymbol{b}$ - 6



27 x (16 – 15)



You're doing great!

- 2 Try these. Think carefully.
- a  $(3 \times 4) + 8 = x$ x =
- **h** 3b = 3(5 + 1) b =

**b**  $y = 3 + 6 \times 5$  y =

- (17 6)4 = 4xx =
- a = 2 (12 + 36) a =
- $y = (24 4) \div (2 + 3)$   $y = \boxed{}$
- $b = (14 + 10) \div (10 2)$   $b = \boxed{}$
- $4b = 4 + 24 \div 3 + 4$   $b = \boxed{}$

- e  $2x = (2 \times 3) + 10$ x =
- 5x = 29 + 3(4 2)  $x = \boxed{}$

**f**  $4a = 5 + (27 \div 9)$  a = 6

 $a = (27 \div 3)4 + 8$   $a = \boxed{ }$ 

 $y = (24 \div 3) + 7$  y =

# Solve equations using the correct order of operations.

To make sure we carry out calculations in the correct order, we use **BODMAS**.

order

brackets 2(3+4)(or other things means the same e.g. - squares) as  $2 \times (3 + 4)$ 

division

multiplication

addition

subtraction

- Use **BODMAS** to find the missing numbers in these equations.
- (27 + 14) + 8 $\boldsymbol{\chi}$
- b  $48 \div (4 + 2)$ y y
- $14 + 36 \times 3$  $\boldsymbol{a}$
- 8 d 56 ÷  $\boldsymbol{b}$ x 15

- 156 12 x 12
- $(158 + 10) \div 12$ a a
- $372 162 \div 9 = 2x$  $\boldsymbol{\chi}$
- $3b = 42 + 16 \div 4 + 2$  $\boldsymbol{b}$



Good work!

Name.....

Class...... Date......

- 2 Try these. Think carefully.
- a  $(54 + 56) \div (73 62) = x$  $x = \begin{bmatrix} \\ \\ \end{bmatrix}$
- **b** (-4 + 6)18 + 134 = 5y  $y = \boxed{}$
- $a = (-2 6) + (8 \times 7)$   $a = \boxed{}$
- $b = 8^2 \times 2$   $b = \boxed{}$
- e  $x = 6^2 \div (33 3 \times 8)$ x =
- $y = \begin{bmatrix} -8 + 12 + 8 \times 9 = 2y \\ y = \begin{bmatrix} -8 + 12 \\ -12 \end{bmatrix}$

- **h**  $16^2 \div (48 16) = b$  b =
- $y = \begin{bmatrix} 3^2 + 2^2 + (1056 841) = y \\ y = \begin{bmatrix} 3 & 3 \\ 3 & 4 \end{bmatrix}$
- $b = 172 + \frac{16}{4} = 16b$

1 Solve the problems below.

**EXAMPLE** 
$$5x + 4 = x + 12$$

Whatever you do to one side you must do to the other.

# STEP 1

Put the x terms on the same side of the equation by subtracting x from both sides.

$$5x - x + 4 = 12$$

# STEP 3

Put the number terms on the same side of the equation by subtracting 4 from both sides.

$$4x = 12 - 4 = 8$$

# STEP 2

Simplify.

$$4x + 4 = 12$$

### STEP 4

To find the value of *x*, divide both sides by 4.

$$x = 8 \div 4 = 2$$

$$a 7y + 2 = y + 8$$

STEP 1 .....

STEP 2 .....

STEP 3 .....

STEP 4 y =

$$12x + 4 = 9x + 13$$

STEP 1 .....

STEP 2 .....

STEP 3 .....

STEP 4  $\chi = |$ 

# b + 4 = 3b + 14

STEP 1 .....

STEP 2 .....

STEP 3 .....

STEP 4 b =

d 
$$15a + 6 = 9a + 30$$

STEP 1 .....

STEP 2 .....

STEP 3 .....

STEP 4 a =

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2 Have a go at these. Think carefully about the steps.

$$a 34a + 1 = 18a + 17$$

STEP 1 .....

STEP 2 .....

STEP 3 .....

STEP 4 a =



STEP 1 .....

STEP 2 .....

STEP 3 .....

STEP 4  $\chi =$ 



STEP 1 .....

STEP 2 .....

STEP 3 .....

STEP 4  $y = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$ 

d 
$$4a + 82 = 16a + 22$$

STEP 1 .....

STEP 2 .....

STEP 3 .....

STEP 4 a =

$$= 59b + 108 = 16 + 82b$$

STEP 1 .....

STEP 2 .....

STEP 3 .....

STEP 4 b =

$$f 65x + 12 = 49x + 36$$

STEP 1 .....

STEP 2 .....

STEP 3 .....

STEP 4 X =

STEP 1 .....

STEP 2 .....

STEP 3 .....

STEP 4  $\alpha =$ 

$$h 12y + 73 = 56 + 16y$$

STEP 1 .....

STEP 2 .....

STEP 3 .....

STEP 4 y =

Name...... Date...... Date......

3 Now try these. You will need to remember **BODMAS** as well.

a 
$$(12a + 4a) + 27 = 6a + 67$$

STEP 1

STEP 2 .....

STEP 3 .....

STEP 4 a =

$$b (4x + 2x) + 4 = 4x + 8$$

STEP 1 .....

STEP 2 .....

STEP 3 .....

STEP 4  $\mathcal{X} =$ 

34y + (2+1)4 = 76 + 2y

STEP 1 .....

STEP 2 .....

STEP 3 .....

STEP 4 y =

(3 + 5)4 + 8b = 14b + 8

STEP 1 .....

STEP 2 .....

STEP 3 .....

STEP 4 a =

### Page 1

**1a)** 5 **b)** 7 **c)** 61 **d)** 43 **e)** 113 **f)** 112

2a) 4 b) 19 c) 8 d) 99 e) 112 f) 195

3a) 62 b) 88 c) 61 d) 178 e) 264 f) 387

### Page 2

1a) 54 b) 264 c) 52 d) 79 e) 182 f) 1253

2a) 79 b) 64 c) 203 d) 136 e) 6841 f) 2374

3a) 222 b) 280 c) 251 d) 424 e) 1082 f) 4726

#### Page 3

**1a)** Example **b)** correct combinations of 85, 33 & 52 **c)** correct combinations of 144, 24 & 168

d) correct combinations of 127, 83 & 44

### Page 4

e) correct combinations of 423, 68 & 491

f) correct combinations of 423, 141 & 282

g) correct combinations of 306, 124 & 430

h) correct combinations of 588, 431 & 157

#### Page 5

**1a)** Example **b)** correct combinations of 165, 63

& 102 c) correct combinations of 432, 51 & 483

d) correct combinations of 364, 153 & 211

#### Page 6

e) correct combinations of 356, 506 & 862

f) correct combinations of 722, 336 & 386

g) correct combinations of 4723, 276 & 4999

h) correct combinations of 6032, 1382 & 4650

#### Page 7

**1a**) 56 – 23 **b**) 86 – 25 **c**) 43 + 14

#### Page 8

2a) 56 + 27 b) 83

3a) £3.50 + £5.00 b) £8.50

### Page 9

4a) appropriate equation e.g. 82 - 65 = 17

**b**) appropriate equation e.g. 79 - 23 = 56

c) appropriate equation e.g. 126 - 42 = 84

### Page 10

**1a)** 182 - 73 **b)** 473 + 189 **c)** 256 - 79

#### Page 11

**2a)** 1652 - 967 **b)** 685

**3a)** 1908 - 1184 **b)** 724

#### Page 12

4a) appropriate equation e.g. £375.50 + £50.78

= £426.28 **b)** appropriate equation e.g. 156.35

-78.5 = 77.85 c) appropriate equation e.g.

87 km + 87 km = 174 km

### Page 13

1a) 6 b) 5 c) 12 d) 6 e) 15 f) 12

2a) 27 b) 24 c) 8 d) 35 e) 12 f) 72

3a) 8 b) 42 c) 9 d) 260 e) 12 f) 98

### Page 14

1a) 7 b) 13 c) 12 d) 18 e) 52 f) 30

2a) 96 b) 11 c) 2280 d) 4 e) 1008 f) 4823

**3a)** 31 **b)** 966 **c)** 12 **d)** 1056 **e)** 16 **f)** 1512

#### Page 15

1a) example b) correct combinations of 54, 9 & 6

c) correct combinations of 12, 8 & 96

d) correct combinations of 78, 6 & 13

### Page 16

e) correct combinations of 13, 15 & 195 f) correct combinations of 153, 9 & 17 g) correct combinations of 23, 12 & 276 h) correct

combinations of 72, 8 & 9

#### Page 17

- **1a)** Example **b)** correct combinations of 322, 14 & 23 **c)** correct combinations of 14, 16 & 224
- d) correct combinations of 345, 23 & 15

### Page 18

- e) correct combinations of 17, 26 & 442
- f) correct combinations of 1352, 26 & 52
- g) correct combinations of 25, 32 & 800
- h) correct combinations of 1176, 56 & 21

### Page19

**1a)** £27  $\div$  3 **b)** 10 x 8 **c)** £2.50 x 6

#### Page 20

- 2a) 9 x 12 b) 108
- **3a)**  $56 \div 8$  **b)** 7

### Page 21

- 4a) appropriate equation e.g. £12  $\div$  £6 = £2
- **b)** appropriate equation e.g.  $23 \times 3 = 69$
- c) appropriate equation e.g.  $27 \times 6 = 162$

#### Page 22

**1a)** £21.70 ÷ 7 **b)** £1.50 x 56 **c)** 592 ÷ 16

#### Page23

- 2a) 21 x 18 b) 378
- **3a)** 56 x 55g **b)** 3080g

#### Page 24

- 4a) appropriate equation e.g.  $768 \div 12 = 64$
- **b)** appropriate equation e.g.  $98 \times 32 = 3136$
- c) appropriate equation e.g.  $872 \times 22 = 19184$

#### Page 25

- **1a)** 21 **b)** 19 **c)** 69 **d)** 30
- 2a) 30, b) 3 c) 75 d) 4
- **3a)** 72 **b)** 33 **c)** 144 **d)** 9 **e)** 39 **f)** 288 **g)** 102 **h)** 8

#### Page 26

- 1a) 24 b) 63 c) 87 d) 63
- **2a)** 135 **b)** 8 **c)** 648 **d)** 7
- 3a) 207 b) 90 c) 2430 d) 9 e) 198 f) 9720
- **g)** 342 **h)** 30

### Page 27

- 1a) 3 b) 23 c) 42 d) 88
- **2a**) 8 **b**) 9 **c**) 12 **d**) 90
- 3a) 72 b) 48 c) 11 d) 7 e) 2 f) 79 g) 100 h) 105

#### Page 28

- **1a)** 56 **b)** 87 **c)** 55 **d)** 346
- 2a) 3 b) 13 c) 6 d) 936
- 3a) 69 b) 1082 c) 12 d) 6615 e) 463 f) 1134
- **g**) 2092 **h**) 8715

### Page 29

- 1a) 17 b) 22 c) 6 d) 12 e) 20 f) 24 g) 9 h) 52
- i) 11 j) 54 k) 16 l) 66

#### Page 30

- **2a)** 8 **b)** 7 **c)** 30 **d)** 3 **e)** 12 **f)** 77 **g)** 4 **h)** 392
- i) 19 j) 4 k) 15 l) 120

### Page 31

- **3a)** 22 **b)** 29 **c)** 4 **d)** 24 **e)** 9 **f)** 67 **g)** 4 **h)** 15
- i) 150 j) 2 k) 222 l) 648

### Page 32

- **4a)** 9 **b)** 93 **c)** 17 **d)** 512 **e)** 8, 102 **f)** 89,168 **g)**
- 12, 2 h) 105, 25

# Page 33

- 1a) 29 b) 65 c) 13 d) 108 e) 79 f) 163 g) 14
- h) 46 i) 84 j) 23 k) 22.75 l) 524.5

#### Page 34

**2a**) 62 **b**) 2394 **c**) 8112 **d**) 16 **e**) 33.2 **f**) 124.9 **g**) 1.25 **h**) 5880 **i**) 694.2 **j**) 3.5 **k**) 122.58 **l**) 336

### Page 35

**3a)** 62 **b)** 199.5 **c)** 62 **d)** 31689 **e)** 56 **f)** 90.46 **g)** 17 **h)** 22.32 **i)** 12864 **j)** 35 **k)** 5907 **l)** 491.13

### Page 36

**4a**) 34 **b**) 6384 **c**) 15.77 **d**) 285.6 **e**) 2, 93.64 **f**) 34.36, 953.37

### Page 37

1a) 16 b) 52 c) 8 d) 114 2a) 28 b) 8 c) 26 d) 89 e) 44 f) 72 g) 105 h) 56

#### Page 38

**3a)** 11 **b)** 9 **c)** 5 **d)** 42 **e)** 6 **f)** 121 **g)** 12 **h)** 9 **4a)** 26 **b)** 91 **c)** 12 **d)** 96 **e)** 8 **f)** 43 **g)** 67 **h)** 12

#### Page 39

1a) 83 b) 18 c) 9 d) 287 2a) 105 b) 145 c) 305 d) 505 e) 239 f) 611 g) 1219 h) 718

### Page 40

**3a)** 19 **b)** 15 **c)** 26 **d)** 742 **e)** 38 **f)** 40 **g)** 53 **h)** 2124 **4a)** 780 **b)** 717 **c)** 37 **d)** 19113 **e)** 5 **f)** 38.8 **g)** 78.6 **h)** 84

#### Page 41

1a) 11 b) 11 c) 14 d) 27 2a) 4 b) 16 c) 16 d) 9 3a) 4 b) 43 c) 14 d) 21 e) 96 f) 37

### Page 42

**4a)** 8 **b)** 8 **c)** 5 **d)** 7 **5a)** 3 **b)** 30 **c)** 5 **d)** 54 **6a)** 4 **b)** 6 **c)** 5 **d)** 36 **e)** 28

### Page 43

**7a)** 42 **b)** 96 **c)** 89 **d)** 12 **e)** 211 **f)** 12 **g)** 20 **h)** 71 **i)** 31 **j)** 10 **k)** 9 **l)** 5

### Page 44

1a) 145 b) 114 c) 261 d) 180 2a) 122 b) 488 c) 272 d) 591 3a) 309 b) 457 c) 207 d) 565 e) 959 f) 1215

#### Page 45

**4a**) 12 **b**) 13 **c**) 14 **d**) 190 **5a**) 34 **b**) 666 **c**) 112 **d**) 351 **6a**) 948 **b**) 31 **c**) 21 **d**) 56 **e**) 126

### Page 46

7a) 407 b) 2496 c) 832 d) 56 e) 248 f) 42 g) 426 h) 423 i) 811 j) 3 k) 3151 l) 22.3

#### Page 47

1a) 7cm b) 20m c) 26mm d) 72km 2a) 6km b) 12cm c) 75m d) 12mm 3a) 61m b) 53km c) 8cm d) 56m e) 5mm f) 13m

#### Page 48

1a) 124cm b) 195m c) 220mm d) 87km
2a) 105km b) 432cm c) 13m d) 16mm
3a) 225m b) 1210km c) 35cm d) 7776m
e) 7.1cm f) 7m

#### Page 49

1) 6cm 2) 10m 3) 3mm 4) 100m

## Page 50

1) 5mm 2) 47cm 3) 4.5m 4) 5.2km

### Page 51

1a) 2,2 b) 2,1 c) 3 d) 3,1 e) triangle

#### Page 52

**2a)** A = -1,1 B = 1,1 **b)** 1, -1 **c)** 2,1,0,-1, or -**2)** 

### Page 53

**1a)** A = 1,1 B = 2,2 C = 5,2 **b)** 4,1 **c)** 2 **d)** 3,1, 4,2, or 5,3

### Page 54

**2a)** A = -1,1 B = 1,1 D = -2,-1 **b)** 2, -1 **c)** E = 1,2 and F = -1,2:1,0 and -1, 0:1, -1 and -1,-1 or 1,-2 and -1,-2

### Page 55

1) 85° 2) 120° 3) 60° 4) 140°

#### Page 56

1) 59° 2) 98° 3) 45° 4) 88°

### Page 57

**1a)** 12cm<sup>2</sup> **b)** 54m<sup>2</sup> **c)** 460mm<sup>2</sup>

2a) 3cm b) 7m c) 2cm

3a) 6cm<sup>3</sup> B) 1m C) 6mm D) 3cm

#### Page 58

4a) 4cm B) 48m<sup>2</sup> C) 9mm

5a) 7cm<sup>2</sup> B) 4cm C) 4m

6a) 8cm B) 6m C) 12cm D) 26m

### Page 59

**7)** Triangle - 44°, Quadrilateral - 85°, Square – all 90°, Pentagon - 100°, Regular Pentagon – all 108°

### Page 60

1a) 104cm<sup>2</sup> b) 243m<sup>2</sup> c) 299mm<sup>2</sup>

2a) 7cm b) 42m c) 21cm

3a) 2cm B) 432m<sup>3</sup> C) 12mm D) 9cm

## Page 61

**4A)** 13cm **B)** 240m<sup>2</sup> **C)** 17mm

**5A**) 116cm<sup>2</sup> **B**) 120cm **C**) 62m

**6A**) 114m **B**) 620cm **C**) 132.5m **D**) 14.5cm

### Page 62

**7)** Triangle – 39.5°, Equilateral Triangle - all 60°, Square – all 90°, Pentagon - 91°, Regular Pentagon – all 108°

### Page 63

8a) 1260°, 140° b) 1440°, 144 c) 8(octagon), 135°
d) 115° e) any appropriate combination = 540°

### Page 64

**1a)** add 5: 29, 34, 39 **b)** add 9: 63, 81, 99 **c)** subtract 11: 56, 23, 12 **d)** subtract 3: -7, -10, -13 **e)** subtract 25: 100, 25, -25

#### Page 65

**2a**) multiply by 2 or double: 16, 64, 128 **b**) multiply by 4: 256, 1024, 4096 **c**) divide by 3: 81, 3, 1 **d**) divide by 2 or half: 40, 10, 5 **e**) multiply by 5: 25, 125, 625 **f**) multiply by 2 or double: 20, 40, 80

#### Page 66

3a) increase, 1, add: 22, 28, 35 b) increase, 1, subtract: 15, 10, 4 c) decrease, 1, add: 36, 42, 47
4a) increase difference by 2 and add: 17, 26, 37
b) decrease difference by 1 and subtract: 16, 10, 5

### Page 67

**5a)** square numbers: 16, 36, 49 **b)** prime numbers 11, 19, 23

**6a)** add 1, subtract 2: 3, 1, 2 **b)** add 5, add 4: 26, 30, 35 c) subtract 5, add 2: 14, 16, 11

### Page 68

**1a)** add 7: 75, 89, 96, 103 **b)** subtract 11: 117, 84, 73, 62 **c**) add 3: 23, 26, 32, 38 **d**) add 3: -6, 3, 6, 15 **e)** subtract 10: 55, 45, 25, 15, -5

### Page 69

**2a)** multiply by 2 or double: 8, 16, 64, 256 **b)** multiply by 3: 24, 648, 5832 **c**) divide by 2 or half: 88, 22, 2.75 **d**) multiply by 2 or double: 0.5, 2, 8, 16 e) divide by 2 or half: 24, 6, 3, 0.75 f) divide by 2 or half: 8, 4, 1, 0.125

## Page 70

**3a)** increase, 1, subtract: 55, 46, 41, 28 **b)** decrease, 1, add: 32, 39, 45, 50, 54 4a) increase difference by 1 and subtract: 8, 1, -10, -17 **b)** decrease difference by 1 and subtract: 48, 18, 15, 13 c) increase difference by 1 and subtract: 4, -6, -17, -24

# **Page 71**

**5a**) square numbers: 1, 9, 25, 36, 64 **b**) prime numbers 31, 29, 23, 17, 13, 11

**6a)** add 4, subtract 8: 13, 9, 1, -3

**b)** double, subtract 2: 26, 52, 50, 100, 98 **c)** multiply by 3, add 2: 51, 159, 161, 483, 485

### Page 72

1a) 
$$(5 \times 3) + 1 = 16$$
 b)  $(2 \times 3) + 1 = 7$  c)  $(9 \times 3) + 1 = 28$  d)  $(10 \times 3) + 1 = 31$  e)  $(1 \times 3) + 1 = 4$  f)  $(12 \times 3) + 1 = 37$   
2a)  $(1 \times 5) + 3 = 8$  b)  $(3 \times 5) + 3 = 18$  c)  $(5 \times 5) + 3 = 28$  d)  $(8 \times 5) + 3 = 43$  e)  $(10 \times 5) + 3 = 53$  f)  $(14 \times 5) + 3 = 73$ 

### Page 73

Page 73

1a) 
$$(12 \times 7) + 3 = 87$$
 b)  $(15 \times 7) + 3 = 108$ 

2a)  $1^2 \times 2 = 2$  b)  $7^2 \times 2 = 98$  c)  $10^2 \times 2 = 200$ 
d)  $12^2 \times 2 = 288$ 

3a)  $4^3 - 8 = 56$  b)  $5^3 - 8 = 117$  c)  $1^3 - 8 = -7$  d)  $2^3 - 8 = 0$ 
4)  $(1 \times 9) -20 = -11$ ,  $(2 \times 9) -20 = -2$ ,  $(3 \times 9) -20 = 7$ ,  $(4 \times 9) -20 = 16$ ,  $(5 \times 9) -20 = 25$ 

#### Page 74

**1a**) circle round 16 - x = 7 **b**) circle round  $y = 208 \div 8$  c) circle round 18 = 7 + xd) circle round  $\pm y = \pm 4 - \pm 1.50$ 

#### Page 75

# Page 76

**1a**) circle round x = 56 + 127 **b**) circle round  $252 \div 14 = y$  c) circle round £4.50 x 4 = b **d**) circle round 1364 + 956 = a

#### Page 77

**2a)** 
$$a = 1486 - 652 = 834$$
 **b)**  $b = 876$   $x = 2628$  **c)**  $x = £24.45 \div 3 = £8.15$  **d)**  $y = £2.64 + £1.25 + £15.72 = £19.61$ 

### Page 78

1a) 10 b) 32 c) 6 d) 5 e) 8 f) 6 g) 40 h) 22 2a) 3 b) 2 c) 5 d) 4 e) 46 f) 72 g) 11 h) 10

### Page 79

**3a**) 4 **b**) 49 **c**) 3 **d**) 42 **e**) 11 **f**) 33 **g**) 2 **h**) 37 **4a**) 36 **b**) 75 **c**) 4.8 **d**) 621

### Page 80

1a) 41 b) 168 c) 6 d) 14 e) 2 f) 189 g) 52 h) 487 2a) 484 b) 28616 c) 2189 d) 2.5 e) 8089 f) 1288 g) 4148 h) 24.8

### Page 81

**3a)** 89 **b)** 88 **c)** 9 **d)** 2460 **e)** 16 **f)** 4934 **g)** 23 **h)** 16.86 **4a)** 2 **b)** 48.439 **c)** 85.236 **d)** 390.18

### Page 82

1a) 4 b) 4 c) 12 d) 18 2a) 20 b) 9 c) 3 d) 63 e) 8 f) 2

### Page 83

3a) 8 b) 4 c) 39 d) 8 4a) 4 b) 6 c) 6 d) 21 e) 8 f) 22

### Page 84

5a) 5 b) 3 c) 4 d) 4 e) 70 f) 10 6a) 6 b) 3 c) 44 d) 3

#### Page 85

**1a**) 37 **b**) 6 **c**) 27 **d**) 36 **2a**) 85 **b**) 35 **c**) 5 **d**) 1080 **e**) 211 **f**) 2

### Page 86

**3a)** 602 **b)** 62 **c)** 1012 **d)** 317 **4a)** 5 **b)** 82 **c)** 13 **d)** 4509 **e)** 3 **f)** 378

### Page 87

**5a)** 98 **b)** 214 **c)** 14 **d)** 13 **e)** 3536 **f)** 42 **6a)** 5.5 **b)** 232 **c)** 308 **d)** 1.5

### Page 88

1a) answers from 1 x 24, 2 x 12, 3 x 8, 4 x 6 b) appropriate answers c) appropriate answers
d) appropriate answers e) answers from 1 x 36, 2 x 18, 3 x 12, 4 x 9, 6 x 6 f) appropriate answers
g) appropriate answers h) appropriate answers

### Page 89

2a) 1 x 28, 2 x 14, 4 x 7 b) 1 x 40, 2 x 20, 4 x 10, 5 x 8 c) appropriate answers d) appropriate answers e) appropriate answers f) appropriate answers

#### Page 90

**3a)** 1 + 5, 2 + 4, 3 + 3, 4 + 2, 5 + 1 **b)** 1 x 12, 2 x 6, 3 x 4, 4 x 3, 6 x 2, 12 x 1 **c)** 10 + 20, 11 + 19, 12 + 18, 13 + 17, 14 + 16, 15 + 15

#### Page 91

h) appropriate answers

1a) answers from 1 x 96, 2 x 48, 3 x 32, 4 x 24, 6 x 16, 8 x 12 b) appropriate answers c) appropriate answers d) appropriate answers e) answers from 1 x 110, 2 x 55, 5 x 22, 10 x 11
f) appropriate answers g) appropriate answers

### Page 92

2a) answers from 1 x 156, 2 x 78, 3 x 52, 4 x 39, 6 x 26
b) 1 x 250, 2 x 125, 5 x 50, 10 x 25
c) appropriate answers
e) appropriate answers
f) appropriate answers

### Page 93

14 + 2, 13 + 3, 12 + 4, 11 + 5, 10 + 6, 9 + 7 **b**) 1 x 20, 2 x 10, 4 x 5, 5 x 4,  $10 \times 2$ ,  $20 \times 1$  **c**) 20 + 20, 21 + 19, 22 + 18, 23 + 17, 24 + 16, 25 + 15

### Page 94

**1a)** 13 **b)** 5 **c)** 52 **d)** 9 **e)** 3 **f)** 31 **g)** 46 **h)** 27

### Page 95

2a) 20 b) 33 c) 96 d) 3 e) 8 f) 2 g) 5 h) 6 i) 11 j) 4 k) 4 l) 7 m) 11 n) 6

### Page 96

**1a)** 49 **b)** 8 **c)** 122 **d)** 105 **e)** 12 **f)** 14 **g)** 177 **h)** 16

#### Page 97

2a) 10 b) 34 c) 4 d) 128 e) 4 f) 5 g) 38 h) 8 i) 1140 j) 283 k) 11 l) 12 m) 21 n) 2045

### Page 98

1a) appropriate steps, 1

b) appropriate steps, 2

c) appropriate steps, 3

d) appropriate steps, 4

### Page 99

2a) appropriate steps, 1

b) appropriate steps, 6

c) appropriate steps, 2

d) appropriate steps, 5

e) appropriate steps, 4

f) appropriate steps, 1.5

g) appropriate steps, 2.5

h) appropriate steps, 4.25

# Page 100

3a) appropriate steps, 4

b) appropriate steps, 2

c) appropriate steps, 2

d) appropriate steps, 4