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Rotate this page to prove to your eyes that five different patterns are encoded, for if you sing beyond them, repeating cyclically on every sixth tone, your ears will tell you they become one happy, extended pentatonic family. We are in Egypt's heaven and among the stars in Plato's. Here is the selfdiscipline toward which Zeus hoped that Atlantis—threatening all of Europe and Asia with its aggrandizement--might be turned. He never had to describe the flood, for many others had written that story. CRITIAS stands finished, as it is, halting in mid-sentence while Zeus considers his options ...

Figure 2

33 We study Atlantis anew to see what Zeus thought the options were for a political philosophy 34 developed "as argument mixed with music." The main problem, Plato thought, was in Zeus himself, and 35 not in the founding of Atlantis, as I mistakenly assumed four decades ago. Homer had given the Greeks a 36 troubled pantheon in which the male leader's spontaneity, particularly in "The Most Beautiful Meeting" 37 with women, whether divine or human (to use the gracious metaphor of EDFU), was the worst possible 38 example for mankind. Notice that Poseidon is sufficiently restrained for the birth of five pairs of twin sons 39 from the same woman. Zeus is a foreign god. imported into Greece from somewhere further East, and his 40 own birth as a son of Kronos ('Time') had been delayed by that grim tyrant's habit of swallowing his own

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- 41 male sons out of fear that one might displace him someday. And that's what
- happened, naturally. Zeus had been brought to birth by a trick of his mother's, andwhen he found a chance he severed the paternal genitals to secure his own
- 44 position, as Kronos had done before him. (Remember that for Pythagoreans the
- 44 position, as kronos had done before him. (Remember that for Pythagoreans the 45 first example of anything becomes the 'algebraic' model (i.e., pattern) for all the
- replications that follow, as we all tend to assume anyway, and Plato's deity never
- 40 replications that follow, as we all tend to assume anyway, and Flato's deity never 47 makes more than one of anything. (The second example proves he got the first one
- 48 right. This assumption can get anybody else into trouble, and you have a right to
- 49 be nervous about it.) Plato assumes that time can reverse instantly under alternate reigns of Zeus and
- 50 Kronos, as two examples in a row illustrate. But neither Egypt nor Plato had any quarrel with time, and I
- 51 hasten to offer a counter-model here as far more appropriate to understanding the Driscoll/Kurtz view of
- 52 Egyptian Genesis.

53 The 12 sharply-pointed teeth in Figure 3 each holds a lotus blossom pointing to the left except 54 that one is turned oppositely at about 5:30 in the local cosmic clock to face its neighbor at about 36:30 as

- 55 seventh—clearly focusing on the problematic square root of 2 at 6:00 o'clock,
- essential to 12-tone symmetry when the "zero hour" is 12:00. Telling timefrom your own shadow was about the only math needed in ancient Egypt, and
- it gave you a pretty good hint. We merely assume that viewpoint is intended
- 59 to be "from the throne of heaven" (with Er in Plato's REPUBLIC and Isaiah
- 60 in the Bible), lying "above the circle of the earth," and count to the right with
- 61 the local clock as if the other eleven lotuses opened in the wrong direction.
- 62 This merely means that in our northern hemisphere the sun—who "sees
- 63 everything" according to the ancients-- *appears* to move to the left, and this
- 64 confuses a lot of people. Socrates had made this locus at 6:00 (directly below 65 Distance hours' of 12:00) at the bottom of a metrical diameter (almost a contract of the second sec
- Plato's "zero hour" of 12:00) at the bottom of a vertical diameter (always in motion, of course) the subject of his dialogue with a slave boy in THEAETETUS by proving that the uneducated lad's soul--descended
- directly from heaven--already could intuit that doubling the area of a square happens on the square of its diameter.² (This was the admissions test for his Academy.) The cyclic octave 2:1 is "a sort of identity" in
- 69 Pythagorean musicology so that its *proportional half* is defined by the square root of 2-- not yet
- recognized as a "number" in Plato's Greece in the 4th century BCE.³ The 'pseudo-identity' of
- halving and doubling introduces a musical "trick" (or rather many tricks) into arithmetic that
- permit astonishing short-cuts for the initiated, but reduces others to wonder, and sometimes
 fury.
- 74





The image in Figure 3 is a Persian relic from the ruins of a city built by descendants of Genghis 76 77 Khan c. 1300 CE and conveys the right feeling for Egyptian pride in its very long history—prospering 78 always from the annual retreating flood waters of the Nile that would have discouraged a less clever 79 people from building there. The country had made a virtue of its 'timely' disaster, transforming it into a 80 blessing. The seven smallest circles in the very middle (on the hub or axle of the wheel) are the ancient 81 Sumerian symbol for 7 as imprinted in damp clay with the round end of a reed stylus. The six largest 82 triangles emanating from the hub lie on three diagonals terminating in "valleys" between the teeth-83 conveniently locating six alternate wholetones lying between 'peaks and valleys' in the gears, and thus identifying the angular positions of 12 equal *chromatic* semitones. Twelve middle size arrows divide the 84 85 model octave 2:1 into 24 quartertones, while 24 smallest triangles further subdivide it into 48 'commas' 86 within which we 'lose our bearings.' (We can identify "a comma" under laboratory conditions, but only 87 rarely in performance.) The "wheel" sums, by counting, as much arithmetic as a musician ever really 88 needs for a *ritual musicology* day or night. The comma is about a quarter of a semitone and thus coincides 89 with the quarter hour as minimal period required to identify the movement of a planet in naked eye 90 astronomy. "Perfect" agreement is always coincidence, discovered in nature when the term is used broadly to include our observation. The 12 lotus blossoms testify to a "Beautiful Meeting" in somebody's 91 92 soul, whether East or West. "Vector analysis" as "mantles of radiance" for the sun god could not have 93 been simpler in any civilization after the fourth millennium BCE. Observatories of any kind anywhere are part of the game as long as sun and moon continue their habits and somebody is around to notice them. 94 95 Symbolically they are the right and left eyes of Egypt's guardian falcon, if you don't mind being called a 'mystic.' (Lover seems more accurate.) What could be more beautiful to teach a child about his 96 inheritance? But Platonic "social science" is studied within a wider context of twelves. 97 "What twelve *is*" in harmonic mythology 98

Not until Kilmer, Crocker and Brown published the decoding (by an international team of
 musicologists) of Old Babylonian tuning theory (1900-1600 BCE) in 1976 did we learn that "12" was
 based on an intensive study of *thirteen*, grouped in successive heptatonic (7-tone subsets) in agreement
 with our naming letters today, but *in tuning order rather than in Greek scale order!*⁴

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- 104
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"Sounds From Silence"--tuning theory 1900-1600 BCE



106 The Egyptian heaven had to have been discovered *within* the great "spiral" of twelve consecutive 107 musical *fifths* of 2:3--alternating with fourths of 3:4--before any part of it really could be understood very 108 deeply.⁵ China had done it more simply, perhaps about the same time, in the Shang dynasty, and without. 109 a word of explanation. Notice how the slanting lines connect the tones here.



Rising fifths alternate with falling fourths from left to right, and *intervals* reverse from right to left. Count them to discover that 1-3-5-7-9-11 are six odd-numbered "males" defining a wholetone scale. Count them again to confirm that 2-4-6 and 8-10-12 also rise (or fall) by wholetones as "female" even numbers

117 (significant only for keeping results compressed for our convenience).⁶

118 And then applaud the *trigrams* and *hexagrams* of the *I CHING* for silently

119 picturing the result with six solid lines and/or six broken lines (as "male +

female"), especially if you have a prurient interest in the sex of numbers, and Plato's Academy was obsessed with nothing else. (Philosophy was essentially a 'cover".) Thus 8x8 = 64 Chinese symbols save

122 a lot of Greek verbal explanation, and encourage adventure, and Egypt loved *economy*. How else could

123 massive temples to the gods seemed appropriately large enough? Egypt was blessed by its floods.

And three, all else.

124 The *TAO TÊ CHING* makes the arithmetic even easier. Chinese common sense, this time directly 125 from the first verse of the 42^{nd} chapter of the TAO TE CHING, preserves sanity and calms the soul while 126 hiding its own far greater genius to be unveiled later.

- 127The Way begot one,128And the one, two:
- 129 Then the two begot three
- 130

131 These few words capture the essence of a pentatonic 132 tuning descending from about 700 BCE and assumed to be 133 inherited from far earlier Shang times. Its algorithm for the pentatonic scale begins, "Take 3 four times," as if 3x3x3x3 =134 135 81 is all you need to do. But there is a verbal "boomerang" in 136 its second part. Assuming now that we are smart enough to 137 reverse direction *boustrophedon* ("as the ox ploughs") $\leftarrow \rightarrow$, 138 at the end of a furrow, the instruction finishes even more 139 cryptically: "add or subtract one-third." Study Table 1 to notice 140 that we can do this in five different ways to define our five 141 different pentatonic modes by the largest necessary integers 142 (81, 96, 108, 128, 144.) Nothing more need be said. The trick 143 lies in the "bull" of 81 that needs to be corralled for four other 144 modes.

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Pentatonic (5-tone) development

Ξ

"Take 3 four times" to begin					
1	3	9	27	81	
64	48	72	54	81	
64	96	72	108	81	
128	96	144	108	81	
64	96	72	54	81	
128	96	72	108	81	
	1 64 64 128 64	1 3 64 48 64 96 128 96 64 96	1 3 9 64 48 72 64 96 72 128 96 144 64 96 72	1 3 9 27 64 48 72 54 64 96 72 108 128 96 144 108 64 96 72 54	

Read each row 🗲 as "add or subtract one-third"

within an "octave double" defined as 2:1

Table 1 (Ancient China)

147 The ancient Near East achieves exactly the same result with equal

simplicity and no need for anything as hard as dividing by 3, eagerly

- avoided wherever possible in both the kitchen and carpentry shop. Merely
- set forth 1-3-9-27-81 in the same way, then double every number to the maximum necessary to "corral" the "bull" of 81 in any place you like.
- 151 Tuning *theory* is an intellectual game for which few musicians, most of
- them impoverished, have little time. Royal scribes probably had some
- 154 boring days with nothing better to do.

155 But any series of 5 consecutive numbers in this "quadrupling of 3" 156 itself (a "continued geometric progression" to Plato, and a routine 157 "logarithmic sequence" to ourselves, $3^{0, 1, 2, 3, 4}$ in modern notation), has the 158 same possibilities as any other. And the same methods can be employed to

- extend the series to any limit of interest to the mind, but not without a smile
- 160 from ear to ear, for there is a secret in the twelve that *must* be computed to
- 161 be certain of its existence. The trick concerns the root meaning of
- Heliopolis ("City of the Sun") as "Eight-town," where every night that

163 luminary had to be towed through the underworld back to his rising place

- 164 in the morning--through twelve dangerous gates guarded by serpents of
- awesome length—all of them equivalent to the serpentine rise and fall of

166 musical fifths and fourths in any civilization—and we don't know how to track its historical source.

167 Every single statement attributed to Pythagoras turns out to be a teasing lie, and historians of mathematics

168 have turned out to be eager suckers for the bait, including some of the most famous with the least..

169 The same procedure turns any set of seven consecutive tones into a "tame" heptatonic serpent 170 defining 7 modes corralling a larger "bull" of $3^6 = 729$, essential to Plato as "tyrant" and to Egypt (in 171 Greek eyes only) as tyrannical Pharaoh "in the midst of the Nile." Pharaoh would heard it as a 172 compliment and smiled.

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- 174
- 175

Table 3 Heptatonic quantification

1,024						
512						
256	768					
128	384	1,152				
64	192	576				
32	96	288	864			
16	48	144	432	1,296		
8	24	72	216	648		
4	12	36	108	324	972	
2	6	18	54	162	486	
1	3	9	27	81	243	729

Take 3 six times to define the heptatonic bull of 3^{6} . Double upward \uparrow to corral in 7 modes. Halve downward \checkmark to recover his "seeds."

Development from "below"

Table 2 (Ancient Near East)







176 The Chinese dragon in Figure 3 is the awesome Aphosis of ancient Egypt, secure in the knowledge that

he himself is scribally "endless," that certainty being supported now archaeologically, linguistically, and arithmetically by neighboring civilizations. Any pentatonic or heptatonic subset is merely a "tame

arithmetically by neighboring civilizations. Any pentatonic or heptatonic subset is merely a "tame
serpent," *Lion of the ground*, in Mesopotamian metaphor, carved into the stone mountains of Egypt as a

sphinx, and reported in the charming story of "The Shipwrecked Sailor" dating to about 1500 BCE, with a

181 kingly serpent anticipating the unflappable and loquacious relative who is reprised three times in the

182 Bible. The serpent confirms to Eve that indeed her God has lied to her about the apple; he tricks YHWH

183 into unconscionable treatment of Job, his own most loyal servant; and he returns in the New Testament to

trap Jesus the Savior into a egomantic emphasis on his own importance that is corrected only in his very

185 last breath on the cross, where he finally submits to his destiny. Egyptian and Biblical serpent wins every 186 encounter with man or woman, and their vocabulary and self control is superb..

- 187
- 188

189 Scribal exercise c.1800 BCE 190 Computing exponential increase 191 into billions by doubling and by doubling plus adding 192 0 1 1 193 1 2 3 194 2 4 9 3 8 27 195 4 81 16 196 5 32 243 6 64 729 197 7 128 2,187 198 8 256 6,561 9 512 19,683 199 10 1,024 59,049 200 11 2,048 177,147 4,096 531,441 201 12 13 8,192 1,594,323 202 14 16,384 4,782,969 203 15 32,768 14,348,907 16 65,536 43,046,721 204 17 129,140,163 131,072 205 387,420,489 18 262,144 524,288 3,486,784,401 19 206 20 1,048,576 207 21 2,097,152 22 Table 4 4,194,304 208 23 8,388,608 Foundational 209 24 16,777,216 habits in 210 harmonical 25 33,554,432 mythology 26 67,108,864 211 Framing 27 134,217,728 octaves vs 5ths 212 28 268,435,456 and 4ths 29 536,870,912 30 1,073,741,824

213 Now a *counting* game begins, and readers must be able to get to 12 on their own because "twin 214 sons" also have a "first pair" notated today with "1" as exponent. This requires the throne (Pharaoh's or YHWH's) to be recognized as the "zero power" of any number, including 3. Study this modification of 215 Figure 1 to meet Plato's "five pairs of twin sons" in Atlantis--if only dear little Clito had NOT been 216 specifically "human." The "wings" here belong only to Spiral 5ths, as if "angels from heaven" where they 217 218 belonged to Plato's planets (until later Alexandrians checked him out and found them in the wrong 219 positions). "Human births" via ratios of 5:4 arise when the Serpent is cut at C and E and the three 220 segments are overlapped vertically along the diagonals //// exposing c-sharp and e-flat (in lower case) 221 on one diagonal and c and e on the other. But the rows above and below lie a comma closer to the middle 222 row of "angels" and rulers, and here the difference is noticed in upper and lower case typeface.



225

226

Figure 6

Plato's harmonic schema for Atlantis



227	Table 5. TRINITARIAN COUNTING ("Twin sons")						
228	3^5 3^4 3^3 3^2 3^1 "1" 3^1 3^2 3^3 3^4 3^5						
229	Old Babylonian "regularization" of base 60 notation (1900-1600 BCE) as developed						
230	in Homer made Plato's unique crystallization in Atlantis the "foundation" of both Christianity and Islam while employing only the most ancient "Egyptian arithmetic," likely profiting from Sumerian/Babylonian insight. Atlantis is interrupted to prevent a sixth pair of "twins" from introducing the "Tyrant" as $3^6 = 729$ expressed as 666 meaning 3 to the 6 th power. There was no way this normal						
231							
232							
233	scribal arithmetic could be "hidden" from the literate scribes of neighboring cultures.						

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In this matrix alignment counting to six from the throne in either direction leaves five twins in the other to explain the congress of kings in alternate periods of 6 and 5 years, doing equal honor to odd and even. But it also suggests why first-born Jewish sons get a double inheritance of family assets. Here is the revolution in mathematics that Plato fathered by recognizing what had been going on for thousands of years, preparing the way for Descartes and his colleagues 2000 years later (as Neugebauer and Sachs recognized in 1945).⁸

Each increase by 60 adds another pair of twin sons to the central axis of the matrix. But a 242 numerical coincidence allows C-sharp to appear on the right within the limit of 60^4 =12,960,000. The 243 required physical ambidexterity thus allows $3^{5}=243$ (Abram in Hebrew gematria, until his named is 244 changed to father Isaac) a reciprocal E-flat to complete the maximum symmetry of eleven tones. (Plato 245 favors the Hebrew Magen David *restriction*, with god in the midst of any ten "gathered for prayer," and G 246 247 D A constant (but not C and E). The triangles of the Magen David offer four alternative tunings above 248 and below the central axis as outlined in the "Marriage Allegory" by its factoring into both 3600 squared 249 and 2700x4800. Thus understanding eventually reduces to patterns within the multiplication table for 3x5 "no more than 1,000" for Plato. Table 6 shows fighting men as naked; Table 7 shows all but a few as 250 251 married (i.e., "doubled in value by a good wife"). (Among the Jews, always "left behind with the baggage 252 train" when fighting threatened.) The study of scribal patterns often requires no doubling whatever.



Interlocked triangles in the Magen David suggest the intricate interweaving of factors of 3 and 5 in the two related systems. Numerical doubling for future *scale order* realigns tones into alternate modes in either pentatonic or heptatonic systems. Rotation of the matrix identifies Plato's "children of worse births" too far from the throne row or lacking reciprocals, eliminating the Hebrew Savior as "Cornerstone." He is saved, indeed, however, by an alternate strategy, so that Plato inadvertently confirms that the Christian Savior is fully human as well as Divine.



The Savior is "saved" in Greece and in Greek for Christian theology as "888" meaning $8^3 =$ 274 275 8x8x8 = 512 as the "cornerstone" of Marduk's throne, the "fountain of youth" for Gilgamesh, and as "Osiris enthroned in the Underworld" in Egypt. His reciprocal's naked "musical" identification as fifth in 276 277 the third row at 3x675 = 2025 would require the throne to be doubled into 1,440 to frame the same "octave womb," the "basic miracle of music."¹⁰ This reduces to 45/32 to equal the Savior—with no gain 278 whatever for the detour into excessively large numbers. I suppress here the intricate foundations of this 279 calculation, easily accessible elsewhere.¹¹ All ancient cosmology consists of variations on the Egyptian 280 year for which 720:360 is precise only for the Just tonal model so "easily manipulated," as my own 281 282 advisor in political theory pointed out in a brilliant essay never published.¹²

Greek Apollo, the archer god and kitharist (famed for playing his lyre "upside down" to win a bet 284 285 with a wind player), is more easily approached first through another Homeric nom de plume as Apollo Smintheus, "mouse god," displayed in Table 8. Watch how he uses Egyptian arithmetic, first doubling 286 then adding himself to reach "3" as many times as he pleases, as if he had read the TAO TÊ CHING. Here 287 we goal the way through twelve *intervals* as some anonymous scribe somewhere must have done in the 288 289 fourth millennium BCE, because several kinds of evidence survive in the Narmer inscriptions as 290 "Scorpion King" at the union of Upper and Lower Egypt dating to about 3200 BCE. Notice Apollo's mincing steps as he munches on a Sumerian "grain pile" that extended to the next "double" beyond. 291

		Tab	le 8.	Apoll	o Smir	ntheus a	s "mous	e god" ill	ustrates	how to trip	ole twelve t	imes
	Double downward, then add to itself to identify the next power of "3" and then search for convergence between leading digits in powers of 2 and 3 to discover 2^{19} near 3^{12}											
lead	ing o	ligits	in pov	vers of	2 and 3	to discov	$ver 2^{19}$ ne	ar 3^{12}				
1	2	3	4	5	6	7	8	9	10	11	12	13
A♭	E♭	B⊧	F	С	G	D	А	Е	В	F#	C#	Gŧ
3 ⁰	3 ¹	3 ²	3 ³	3 ⁴	3 ⁵	3 ⁶	37	3 ⁸	3 ⁹	310	311	312
1↓	3↓	9↓	27↓	81↓	243↓	729 ↓	2,187↓	6,561↓	19,683↓	59,049↓	177,147↓	531,441
2 7	6 7	187	54↗	162 7	486 /	1,458 7	4,374 7	13,122	39,366 7	118,098 7	354,294 7	[precession?]

292

293 The Babylonian tuning system in Figure 4 proceeds through all 13 tones before being presented a 294 second time in reverse order, thus anticipating the *precession* of the equinoxes--a 'turning back' in the 295 behavior of the sun as bluntly cryptic as the ages of Zeus and Kronos reverse for Plato. His favorite 296 example of the forces in play at the turning pole in a chariot race demonstrate vividly the Greek sense of 297 dynamic forces of physical Necessity ("Chance," deified for thinkers unfamiliar with the craft) that come 298 into play when "ideal" models are actually "set in motion" as Atlantis was "invented" (inherited?) to 299 display Socrates political models to himself. The musicology may be as old as its celebration in stone circles. The limits of Narmer musicology cannot be confirmed with evidence presently available, but the 300 301 400,000 "sheep" whose capture is celebrated more than suffice for 12 tones in theses sequences. And the 302 120,000 prisoners whose heads he is picture smashing could be the 120,000 Archers, or Hoplites, or 303 Slingers in Plato's Atlantis. And the 1,422,000 goats Narmer captured are certainly Israel's scapegoats for 304 Seth is symbolized by the ratio 64:45 (fifth place in the third row of Figures 7 and 8 when extended by doubling to include him)--meaning 64/45 = 1.422,222 today on our pocket calculators and merely 305 rounded off to the "3 places" preferred by the ancients for "continued fractions."¹³ For a hundred years 306 our possession of the Narmer data would have sufficed to support Egyptian precedence if only we could 307 308 have believed such primitive "animal worshippers" capable of rational thought. We have miss-read 309 history as our own "worst enemies" by our inability to believe that ancestors had "risen from the ape" 310 40,000 years ago. They chose the animals that made the most perfect images of what they wanted to 311 convey. We don't have to rise again, as some seem to think, unless we regress that far.

312

Summary: Apollo as god of music and mathematics

Homeric Apollo could stand on the throne of Egypt at 2^6 =64 and "shoot" accurately and 313 exponentially to either end of this sequence of 12 intervals "between 13 limits" (Plato's description of 314 conditions) by 3^6 , or from one end to the other (and far beyond). Exponential series were no problem and 315 316 great fun before 3000 BCE. The 13 tones of the complete spiral of 5ths and 4ths is cut in two places (c:C and E:e) to produce alternative *heptatonic* (7-tone) 'Just' systems of 3x5 = 15 pitch classes in which two 317 318 are at war for each other's position as Osiris and Seth. They are competing for the throne as a-flat and gsharp in the middle of the octave (the corners of the rhomb). Thus the Horus who reigns as Pharaoh 319 320 eventually also becomes Osiris at death to reign in the Underworld—the Egyptian heaven of delight-- but 321 never free from Seth's competition (to some authors). The whole system inverts day and night, thus "warfare in heaven" never ceases. And the dead Osiris becomes the living Jesus of the New Testament. 322 323 There are many ways to tell these stories.



329 As potential square root of 2 in the precise middle of the octave, a-flat (small case) lies very 330 slightly nearer the throne from *below*, and g-sharp lies very slightly nearer than G-sharp from *above*. Here 331 is the motivation for thousands of years of narrative strife, so subtle that only the arithmetic can illustrate it, and so simple that a child with a pocket calculator can test it in a few seconds. The difference often is 332 333 aurally trivial, except to the idea of absolute perfection as lying beyond the powers of mankind. Great 334 artists have left tokens of their respect (including the very great self-respect implied by leaving some small portion "unfinished"). In Narmer's palette two very long-necked ambiguous quadrupeds coil their 335 336 necks around each other as Seth and Horus confront each other eye to eye. The symbolism is brilliant.

337 The 15 elements of this rhombix constitute the bed of Sumerian Inana (Babylonian Ishtar) as 338 "temple virgin" in Marduk's great temple in Babylon. Tones G and A exchange roles as Poseidon's "first 339 pair of twin sons" (Atlas and Gadirus only because I'm playfully pretending that the Greek gamma means G in this notation, while corresponding to C in our alphabet). Chinese history makes "C" its own Huang-340 341 Chung 'Yellow Bell' emperor in ancient times, imagined as setting the moral tone for his reign, often 342 notably brief. A and G functions always for Plato (in one way or the other) as his harmonic and arithmetic means, leaving the other tones available as "moveable sounds" for whatever pentatonic and heptatonic 343 344 alignments we like. They-belonging to the middle row--are indifferent to rotation by 180 degrees and thus to 'Poseidon's earthquakes" achieved with reciprocal powers of 5. Atlas acquires "his mother's 345 portion" (perhaps as "first-born" among the Jews, depending on who got his hands on this data first). All 346 347 other elements that are equidistant from the throne on straight lines through it are *paired twins*. In the 348 neighboring rows of Just ratios above and below their major and minor thirds 'mapped' along diagonals / 349 and \) share some "points" of coincidence in the "becoming" of six different major and minor *triads* 350 today. In ancient times it probably was not their roles as "secondary consonances" that made them 351 'auxiliary guardians,' but more likely that results then were restricted to 3 digits in base 10 arithmetic (instead of 6 digits, as threatened in Table 8, and correspondingly truncated in base 60). At some point in 352 history 'Ishtar' lost her early status "on the throne" (D) as "god 15) to become Venus as both Morning 353 354 Star and Evening Star, roles formerly belonging to Horus and Seth in Egypt. Plato implies that her new role only recently had been discovered Greece. I notice that her demotion places her in the Savior's 355 favorite manger as "cornerstone," and the book of REVELATION demotes her to oblivion as His light in 356 New Jerusalem, if it ever comes, makes both Sun and Moon superfluous should he ever reappear again. 357 358 We have much to fear, for at that point time is ended and Babylonian musicology silenced.

359 The Horus hawk standing guard before EDFU had a twin (now smashed), and representing the "wings" of the tonal cartouche in Spiral 5ths tuning. He is alter-ego of the Great Serpent below and 360 "merely" reciprocates its arithmetic. AS ABOVE, SO BELOW, the rubric of Mesopotamian cosmology, 361 thus fully agreed with the source of all power, but other cultures toyed playfully with the rhetoric and its 362 363 mathematization (mostly suppressed here). The trapezoidal sides of the towers guarding the entrances to 364 various sections of Egyptian temples are reminders of the geometry useful in taxing quickly and equitably the land refreshed by the annual flooding of the Nile as property lines were restored. All four sides of its 365 pylons lean inward toward the top, and irregular quadratic areas of each side were very simply estimated 366 by squaring half the sum of opposite sides. But perfect "musical solutions" were also readily available 367 when needed by "squaring" some of the corners and computing triangles also with perfect accuracy, as 368 369 we learned from Neugebuer and Sachs only in 1945. Music was never a separate "science," and physical 370 measurement still proves nothing about *musical values*.

The Argo as the "first 50-oared ship" is not a Greek invention but a new Greek metaphor for a 371 372 proportion written as 70:50::49:35 but *read in either direction* to identify the 50th unit that straddles the 373 middle of its "octave-double" as one of the greatest miracles among all the arts and sciences. Only the ear has this divine gift of an inner metric granted at birth, and that middle unit frames the contest of Horus 374 and Seth. The ratio 49:50 is perfectly centered, and the "sacrifice of the Savior" as the unit between two 375 376 "robbers" (one 'good' the other 'bad') is the Jewish drama preserving our heritage of one-percent 377 tolerance--assuming that our behavior otherwise is appropriately "self-disciplined." Socrates died for this 378 principle. Plato dramatizes it as "What 12 is" in Atlantis by summing its armed forces to 1,200,000. 379 Tones G:D:D:A constitute a Platonic Trinity in the only tunings he requires in philosophy and thus turn 380 inside out to frame A and G as his "twin means" with the octave on D defined by 12:9::8:6 which of 381 course can be read forwards or backwards, and applied to rising or falling pitch classes. The pentatonic 382 scale presented in Figure 1 locates our "feet" at 5 and 7 as musicologically 8 and 9, and permits the 383 perfection of modern equal temperament to be "counted" at intervals of either 5 or 7 hours in either 384 direction, or twinned in both directions, from any place we choose, each option requiring its own 385 appropriate arithmetic. The "dance of the hours" is the only dance there is for a *ritual musicology*.

386 Inside the entrance pylons to EDFUR we notice that the large public courtyard is lined with 32 387 pillars, and the unit "1" is "Forgotten Cornerstone" when Table 6 is reconfigured as Table 7, so that $2^5 =$ 32 in the basic 60:30 matrix, and doubles further to 888 as 2^9 =512 in Table 8, the Savior's locus in early 388 Christian symbolism. Moses orders 32 virgins from the Jewish victory over the Midianites to be assigned 389 to the high priest's office (Numbers, chapter 31).¹⁴ We might notice also that 675 "sheep" from 675,000 390 391 captured are assigned to that office and that Figures 6 and 7 require 675 in fourth place in the third row. 392 Also, of 36,000 captured cattle one in fifty go to the Levites in charge of the tabernacle, meaning 393 36,000/50 = 720, just what we need for the ancient Sumerian "brick constant" (no matter size or shape) 394 and thus also for the 50-year Hebrew Jubilee calendar. We haven't time or space to continue here, But 395 most aspects of Jewish arithmetic seem carefully tested for at least a thousand years in Egypt while the 396 alphabet was being invented. And the geometry of the Magen David itself is splendidly represented in 397 synagogues in a configuration suggesting the interwoven complexity of the arithmetic in Figures 6-7-8. 398 All other matrices for "Holy Mountains" with these three primes are expansions or contraction's of Marduk's throne in Figures 7 and 8, inspired by the same "laws" of harmonic "coincidences" as if God 399 400 himself had planned them. And the YHWH is a Hebrew plural paying honest credit to his cultural 401 predecessors, slowly perfecting his role.

402 By inviting us to search for Atlantis at EDFU where the tributes of ten Greek pharaohs suggest 403 they perfectly understood the discipline of Holy Ten-ness (that Plato encrypts into "What twelve *is*") we 404 may indeed be coming closer to Plato's vision, and to his own reverence for the "body" of the world as 405 well as for its soul. At EDFU The public court stops at a path between twelve magnificent pillars like

those painted in the 19th century (see p. 15, looking outward from between
them) before the desert sands were swept away for modern visitors. Beyond
is another court with 12 smaller pillars, as if mimicking or inspiring Plato's
"dyad" (i.e., "two") of "the great and the small." And the darker sanctuary
beyond them is surrounded by 13 "chapels" of which 3 are accessible only
from neighboring spaces, perhaps accidentally suggesting the 13 tones we
had to study to understand the first five.

The armed forces of Atlantis total 1,200,000 as Plato playfully
reminds us that "what 12 *is*" depends on context. ¹⁵ Notice 1,200 "ships" and
not 10 but 10,000 chariots. He is inventing "political theory" with a
"manipulable musical model." All theories come under the rule of *physical*"*Necessity*," with whom not even gods may argue.

Military strength of Atlan	
Archers	120,000
Hoplites	120,000
Slingers	120,000
Javelin throwers	180,000
Light-armed slingers	180,000
Horseman and charioteers	240,000
Sailors	240,000
Total	1,200,000
Ships	1,200
Chariots (1/6 th from each)	10,000

C#

E♭

C#

e♭

D

D

4

419 As an 'archaeomusicologist' of sorts, if allowed so pretentious a title, reviewing "Egyptian 420 Origins" through the eves of Ian and Matt has been a great experience. I think they've got it right, 421 possibly without really knowing it yet. They are reading Atlantis with what I believe to be "the right feeling." They have learned reverence for the beautiful, however mysterious, in their own ways. My own 422 Pythagorean tutors (Siegmund Levarie and Ernst Levy, now both deceased) and I have based our work on 423 that of Albert von Thymus in the late 19th century whose genius in establishing *perspective* was rewarded 424 by the burning of nearly all copies of his work.¹⁶ But notice that across more than 5000 years of written 425 evidence a *theology of music* has never been lost, and is more alive today than ever.¹⁷ "What is not 426 evident from the data presented here is that the Atlantis limit of 12,960,000 as 60^4 is a Platonic reduction 427 428 by a factor of 60 from the prevailing Apollo/YHWH matrix of $60^5 = 777,600,000$ for the highest deity, known to all major civilizations of the ancient Near East during the second millennium BCE. 429

430 431 432 (It must be understood here that the author is drawing on the recent studies, publications, dialogue and direct assistance of many more colleagues than are indicated in the notes, and in ways that must be acknowledge elsewhere and in detail. Interdisciplinary studies in the modern Academy are highly dependent on personal friendships.)

Table 10 Plato's tonal schema for Atlantis through "4:3 mated with 5"

then "thrice increased" to $60^4 = 12,960,000 = 3,600^2 = 2,700 \text{ x } 4,800$

a maximum of two "children of better and worse births" are permitted as

"moveable sounds" but no "enharmonic" relatives (sharing the same names)

b

f

b♭

f#

B♭

F#

В

F

framing fourths of 4:3 are constant within the

musical proportion 12:9::8:6 rising or falling

С

Е

с

e

G#

A۶

a♭

g♯

~ \sqrt{2}

A

G

3

433

434

435

436

437

439 440

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441

442 443 Here is the schema I've always employed, but never presented clearly. It is easier to understand 444 "holistically" than piecemeal, but that requires experience. You may intuit here why it is not easily 445 intuited from the numbers themselves without careful study of narrative context also. I know of no other 446 presentation quite like this, but many theorists have published and many must be aware of this pattern. 447 (Microtonalists have explored extensively.) Plato's arithmetical total was analyzed correctly by James 448 Adam in the early 1900's, cited by Brumbaugh in the 1950's, and saved me at least 20 years of effort. Chinese description seems simplest, Babylonian is brilliantly applied to tuning practice, and Egyptian 449 relics are charming in their conciseness. In general, "laws" are intended to ensure several degrees of 450 451 human freedom, but only when severely "self-disciplined." Pentatonic resources of 5x12=60 "mode keys" (specified in China), for instance, require both "perfect pitch" memory and limitation on the number of 452 453 tones employed and 'rhetorical' emphasis on them or they are perceived as only one "happy family," with 454 little or no modal distinction beween them. 455

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Table 11 Brick alignments to 60-720-2,700- 3,600 -4,800 in Atlantean arithmetic contain 8-18-25-26-27 elements always read with double meanings in base 10, thus escaping the novel notation in base 60.that philosophy avoided. But the matrix is under the contextual discipline of "Necessity" and her daughters, the Fates, always to be feared.

					31	25									
				6	25	18	75								
			1	25	37	75	1,1	25	3,3	75					
		2	5	7	5	22	25	6	75	2,0	025				_
		5		15	4	5	13	35	40)5	1,21	15	3,0	545	
1	1	3	3	0	9	2	.7	8	1	2	43	7	29	2,1	87

Platonic analysis of Atlantis numerology

Figure A9. Only 8 products of 4x3x5<60 remain from Babylonian Ishtar's position as "god 15"



Egyptian fractions need only a small oval ("opening the mouth"?) to indicate reciprocals (integers as divisors).

Figure A10. Paired integers <60 or <120 require multiplication to 12x60=720, but 5 results then prove to be "worse births" or without paired twins in the "upright" male matrix-- and including the "cornerstone" unit from which all emanate as multiples.



Only three central rows can produce useful tones. Horus usually wins as smaller integer at the same ratio.

469	Epilogue
470	The Great Serpent, now deceased?
471 472 473 474 475 476 477 478 479 480 481 482 483 484 485	The upright serpent on the Edenic island in the now popular Middle Egyptian story of "The shipwrecked sailor" is inspiration for the Bible's more loquacious relative some two thousand years later. Driscoll and Kurtz review the story in detail on pages 42 to 48 and include a magical picture of the serpent with sailor prostrate before him on page 45. But in the context of his own time that serpent was a living testament to the influence on Egypt of a Sumerian science in the fourth millennium BCE, two thousand years earlier. It belongs to the foundation of "base 60" arithmetic. All of the 120 sailors assigned the ship were lost except himself, sent as emissary of Pharaoh to "bring back a treasure from the mines"which of course were Sumerian "holy mountain" matrices of integers $2x3x5 < 120$. This limit of 120 is mentioned several times (as both length of the ship and number of sailors). But this eventually is the lifetime in years assigned to mankind in the Bible and exhibited first by Moses in leading the Jews to liberation between his own 80 th and 120 th year. In three books and more than forty essays I've never presented this basic matrix. Here 'tis as an example of Plato's "small and great"—indifferent to being read as integers or their reciprocal unit fractions. The pattern inverts naturally within the Magen David but "ejects" 81 as "supernumerary" lacking a reciprocal (i.e., 81 as Pharaoh's agent) within this limit, and also the unit "1" that generates all numbers and thus is "head of the serpent."
486	Table 12 Man's Lifetime of 120 years
487	25 75 81 27 9 3 1
488	5 15 45 45 15 5 1 3 9 27 81 75 25
489	1 3 9 27 81 75 25
490 491	Notice the preponderant "harmonical" symmetry under "deity" as generative unit and "head" of the serpent within the "octave double" 120:60. Symmetries are the very heart of the Magen David.
492	Table 12 Man's Lifetime of 120 years
493	100 75 b 1#
494	80 120 90 G D A
495	96 72 bb f
496	
497 498 499 500 501 502 503 504	Abraham leaves Haran at 75 to pursue a new life exploring the Holy Land under divine guidance. Moses leads 600,000 Jewish brickmakers to freedom between the ages of 80 and 120, but except for Joshua and Caleb only 40,000 from the next generation enter—under "Magen David" discipline, apparently forgotten about 1200 CE during the Diaspora when the musical content of numerical Kabbalism was lost. Preservation of the texts ensures that much of it remains recoverable. Only immortals are able to "return" (as Gilgamesh learned). Thus the Hebrew deity remains "a pillar of fire by night and a dark cloud by day" as he comes and goes while man learns to survive on faith alone as <i>Jeshurun</i> ("upright").
	¹ Miriam Lichtheim, translator, "The Prayers of a Theban King" in ANCIENT EGYPTIAN LITERATURE, Vol. 1 (Berkeley, University of

¹ Miriam Lichtheim, translator, "The Prayers of a Theban King" in ANCIENT EGYPTIAN LITERATURE, Vol. 1 (Berkeley, University of California press, 1975) p. 95. ² Seyyed Hossein Nasr, *SUFI ESSAYS* (Albany: State University of New York Press, 1985) cover, developed in "Children of Abraham" by

Ernest G. McClain" in SOPHIA (Summer 2009) pp. 59-77.

³ Ernst Levy, A THEORY OF HARMONY (Albany: State University of New York Press, 1985) p. 5.

⁴ Anne D. Kilmer, Richard L. Crocker, and Robert R. Brown, SOUNDS FROM SILENCE (Berkeley, Bit Enki, 1976).

⁵ Richard J. Dumbrill, THE MUSICOLOGY AND ORGANOLOGY OF THE ANCIENT NEAR EAST (London, Tadema Press, 2000).

⁶ Ernest G. McClain, "Tonal Isomorphism in Plato and the *I Ching*" in PLATO, TIME AND EDUCATION, Essays in honor of Robert S. Brumbaugh (Albany: State University Press, 1987) pp. 131-152. ⁷ Jöran Friberg (New Jersey: World Scientific, 2005) Chapter 1.

⁸ Otto Neugebauer and Abraham Sachs, MATHEMATICAL CUNEIFORM TEXTS (New Haven: American Oriental Society, 1945).

⁹ Alexander Heidel, THE BABYLONIAN GENESIS, 2nd edition (Chicago: University of Chicago Press), p. 48.
 ¹⁰ Siegmund Levarie and Ernst Levy, TONE: A STUDY IN MUSICAL ACOUSTICS (Kent State University Press, 1968), p.212.

¹¹ Duane L. Christensen, NAHUM: A NEW TRANSLATION WITH INTRODUCTION AND COMMENTARY (New Haven: Yale University Press, 2009) pp. 25-39. ¹² Harvey Wheeler, "The invention of wisdom: from the discovery of audial psychophysics to Plato's politics" (JOURNAL OF SOCIAL AND

BIOLIGICAL STRUCTURES, Volume 5 No. 3, July, 1982).

¹³ Jöran Friberg, AMAZING TRACES OF A BABYLONIAN ORIGIN IN GREEK MATHEMATICS (World Scientific, 2007) pp 431 trapezoid ¹⁴ Bible, Revised Standard Version, Numbers 31:32-41.

¹⁵ Robert Brumbaugh, PLATO'S MATHEMATICAL IMAGINATION (Bloomington, Indiana University Press, 1954, Kraus Reprint 1968).

¹⁶ Joscelyn Godwin, THE HARMONY OF THE SPHERES (Rochester: Inner Traditions, 1993) pp. 370-381.

¹⁷ Ernest G. McClain, THE MYTH OF INVARIANCE, 1976 and 1984, THE PYTHAGOREAN PLATO, 1978 and 1984, MEDITATIONS THROUGH THE QURAN, 1982 (York Beach, Nicolas Hays).